## PROGRAMMABLE CALCULATOR ET-57



User's Guide

# ET-57 Programmable Calculator <br> User's Guide 

Calculator version 201101
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website:
http://www.breatharian.eu/hw/et57/

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For each key, the basic meaning is shown on the first line and the alternative meaning on the second line of the screen (after pressing the 2nd key).

| $\begin{gathered} {[11]} \\ {[1]} \end{gathered}$ | 2nd | $\begin{gathered} {[12]} \\ {[1]} \end{gathered}$ | INV | $\begin{aligned} & {[13]} \\ & {[18]} \end{aligned}$ | $\begin{aligned} & \ln x \\ & \log \\ & \hline \end{aligned}$ | $\begin{aligned} & {[14]} \\ & {[19]} \end{aligned}$ | $\begin{aligned} & \text { CE } \\ & \text { C.t } \end{aligned}$ | $\begin{aligned} & {[15]} \\ & {[10]} \end{aligned}$ | $\begin{aligned} & \text { CLR } \\ & \text { OFF } \end{aligned}$ |
| :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: |
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| [46] | Nop | [47] | Del | [48] | Fix | [49] | Int | [40] | \|x| |
| [51] | GTO | [07] | 7 | [08] | 8 | [09] | 9 | [55] | X |
| [56] | Dsz | [57] | STO* | [58] | RCL* | [59] | SUM* | [50] | Deg |
| [61] | SBR | [04] | 4 | [05] | 5 | [06] | 6 | [65] | - |
| [66] | $\mathrm{x}=\mathrm{t}$ | [67] | Inc* | [68] | Exc* | [69] | Prd* | [60] | Rad |
| [71] | RST | [01] | 1 | [02] | 2 | [03] | 3 | [75] | + |
| [76] | $\mathrm{x} \geq \mathrm{t}$ | [77] | Inc | [78] | Pgm | [79] | Rand | [70] | Grad |
| [81] | R/S | [00] | 0 | [83] |  | [84] | +/- | [85] | = |
| [86] | Lbl | [87] | $x$ ! | [88] | Stat | [89] | Mean | [80] | Var |



## 2. Features

Summary : Calculation accuracy of 17 mantissa digits (BCD code), 11 mantissa digits displayed. 80 registers (RAM), 500 program steps (EEPROM), ARmega8 processor, LCD screen.

- ATmega8 processor (8 MHz, 8 KB ROM, 1 KB RAM, 512 B EEPROM)
- Supply voltage 5 V (from USB charger or USB port)
- Calculations in BCD code
- 40 key keyboard
- Two-line LCD display ( $2 \times 16$ alphanumeric characters)
- 17-digit calculation accuracy
- Accuracy of base registers 15 digits
- Accuracy of extended registers 13 digits
- Data display to 11 significant digits
- Scientific display mode with exponent on 2 digits, from - 99 to +99
- 10 program spaces
- 50 program steps per space (500 steps total)
- 10 labels per program space
- Function calls and jumps between program spaces
- User program stored in EEPROM (without battery)
- 10 base registers (accessible by direct addressing)
- 70 extended registers (accessible by indirect addressing)
- Indexing access to variables
- Exponential and logarithmic functions
- Trigonometric functions
- Statistical functions
- Factorial
- Random number generator
- Fully open source hardware and software
- Controlling an external device via the ISP connector
- Calculator code entirely written in AVR assembler


## 3. Description

The ET-57 calculator is conceptually based on the famous TI-57 calculator, developed in 1977 by Texas Instruments.
It tries to maintain compatibility with programs written for the TI-57 while extending functionality by utilizing the capabilities of the processor being used.
The functionality is extended by more program spaces (10 spaces for a total of 500 steps), more data registers (80), direct and indirect addressing, factorial, random number generator...

The calculator is intended for former users of the TI-57 calculator, those interested in retro technology, and as a teaching aid to familiarize themselves with the principles of calculator use and programming.
For this reason, they strive to simplify the design as much as possible, consisting only of microswitches, a processor, an LCD screen, a connector for the external power supply and a few small components.
The ET-57 is a tool made for experimenting, teaching, or being used in the office with external power from a USB charger or USB port.

In addition to the basic ET-57 variant with an ATmega8 processor, the calculator can also be available in the hardware variant of the ET-58 calculator, with ATmega88, ATmega168 or ATmega328 processors.
This ET-57B variant differs from the base variant in that it allows the calculator to be turned off (OFF button) and LCD screen contrast control, but does not provide access to external devices (the ET-58 calculator does not include an ISP connector).

## 4. How to use the calculator

The ET-57 calculator is equipped with a 2-line alphanumeric LCD display, 40 microswitches and a processor.

Since the calculator is not battery powered (it is intended for desktop use with external power from a USB charger or USB port), it does not include a power switch. feed.
The user program is stored in the EEPROM memory, the content of which is retained even without power supply.
By disconnecting the power supply, the calculator is reset, the registers, the contents of the display and the operations started are erased, only the contents of the user program (in the EEPROM) remain.

After connecting the power, the calculator name will be displayed on the calculator screen for 1 second, along with a 6 -digit code representing the date of the calculator's firmware version.
For example. "ET-57 201101" means firmware date (build) 11/1/2020.

The calculator in the ET-57B variant (reprogrammed ET-58 calculator processor) can be turned off by pressing $\mathbf{2 n d}$ CLR (function OFF) and turned on by pressing CLR.
By pressing INV 2nd CLR (LCD function) followed by a number from $\mathbf{0}$ to $\mathbf{9}$, the contrast of the display can be controlled.

## 5. Deviations from the TI-57

Although the ET-57 calculator software strives for maximum compatibility with the original TI-57 calculator, deviations may occur and some programs may need to be modified upon import.
Here are the known discrepancies that may need to be taken into account :

## Greater accuracy

The original Tl-57 calculator operates with an internal precision of 11 digits (11 BCD digits of the mantissa, 2 digits of the exponent, 1 digit of the sign, 7 bytes in total) and displays a maximum of 8 digits of the mantissa.
The ET-57 calculator calculates internally with a mantissa precision of 17 digits (10 bytes per number).
It stores the result of the calculation in base registers (i.e. registers RO..R9 and $\mathbf{X}$ ) with a precision of 15 digits ( 9 bytes). When stored in an extended register (R10..R79), data is rounded to 13 digits (8 bytes).

The original TI-57 calculator uses the CORDIC method for function calculations, which allows relatively quick and easy calculations using only basic operations (shift, addition, subtraction) and table values.
The CORDIC method is used in calculators and internally in processors.
In contrast, the ET-57 calculator uses the Taylor series for calculations, which is more suitable for the type of processor used.

As a consequence of the above, the original TI-57 calculates with a precision of 9 to 10 digits, the additional 1 to 2 digits of the mantissa include calculation inaccuracies. ET-57 calculates functions with a precision of 15 digits (internally it calculates to 17 digits, by storing in the register the result is rounded to 15 valid digits).

Higher accuracy is usually not a problem, it can appear, for example, with a random number generator or when comparing the results of calculators.

## Calculation repetition

The ET-57 calculator, after pressing the $=$ key, repeats the last entered arithmetic operation, while on the original TI-57, repeatedly pressing the $=$ key causes an error indication, which some programs use to indicate an error.
In such cases, it is necessary to provide an error indication in another way, for example with the sequence CLR $1 / \mathrm{x}$.

## 6. Numbers format

In the original TI-57 calculator, a number is stored in 14-digit BCD registers D13 to D0. A single digit can take values from 0 to 9 . The lower two digits, D1 and D0, contain the unsigned exponent, ranging from 00 to 99 . The upper 11 digits, D12 to D2, contain the mantissa digits. The mantissa is always left-aligned so that the D12 digit does not contain zeros. The highest digit D13 contains the sign flags. Bit 0 indicates a negative mantissa, bit 1 a negative exponent, and bit 2 an inverted mantissa (highest digit carry sign, mantissa in negative form). This method of interpreting numbers uses CPU support for BCD operations.

The ET-57 calculator also uses a BCD interpretation of a number's mantissa. The BCD format provides more appropriate rounding of results for human interpretation. For example. the number 0.1 is stored in the BCD code as the digit ' 1 ' with an exponent of -1, with no loss of precision. In binary code, such a number would be expressed with the mantissa 4CCCC... (infinite number of digits), when the simple writing of the number creates a small error.

The mantissa is not stored in the ET-57 calculator in absolute form with a separate sign (as in the original calculator), but retains the signed form, with an extension to the most significant digit. A signed digit contains the value 0 (indicating a non-negative number) or 9 (indicating a negative number). The negation of a
number means the "decimal complement" of the digits of the mantissa, or the "nines complement" (= inversion) increased by 1.

The exponent again expresses a decimal exponent, but it is stored in the first byte of the number as a binary number with a bias of 128 . An exponent with a value of 0 (order of ones) is symbolized by the binary value 128 . An exponent of 1 (tens) has a value of 129, an exponent of -1 (tenths) has a value of 127 .
The exponent has a range of valid binary values from 29 to 227 , which corresponds to a decimal exponent from -99 to +99 .
In addition, 3 special cases of exponent values are used: 0 indicates zero, 28 indicates an overflow towards negative exponents (too small number) and 228 indicates an overflow towards positive exponents (too large number).

The calculator uses 3 number formats, differing in the precision of the mantissa:

1) 10-byte numbers (17-digit precision) are used in calculations. The first byte is the exponent in binary form with a bias of 128 . The next 9 bytes contain the mantissa in signed form, from upper digits to lower digits. This means 1 significant digit and 17 significant digits. By displaying the mantissa in HEX form, the figure is displayed in a human-readable form, as numbers from left to right.

The mantissa is normalized so that the first digit (sign) contains 0 (a non-negative number) or 9 (a negative number). The second digit (the highest digit of the mantissa) contains a different number than the signed digit - i.e. the mantissa is left-aligned.
2) The base registers ( $\mathbf{R O}$ to $\mathbf{R 9}$, as well as the $\mathbf{X}$ and LAST registers) occupy 9 bytes ( 15 digit precision). The first byte is the exponent, the next 8 bytes contain 15 mantissa digits and 1 sign digit.
3) The extended registers (R10 to R79) occupy 8 bytes (precision 13 digits), with a mantissa of 7 bytes, i.e. 13 digits of mantissa and 1 digit of sign.

The mantissa of the result can be displayed for debugging purposes with the INV + keys (disabled with INV -). The 16 digits of the X-register are displayed, without the exponent.

Examples of numbers (in HEX format, including an exponent with a bias of 128) :

$$
\begin{array}{r}
3.14159265358979->800314159265358979 \\
-3.14159265358979->809685840734641021 \\
123.456->820123456000000000
\end{array}
$$

A famous trigonometry test can be used to test the accuracy of the calculator:


If the calculation is correct, the result should again be the number 9 .
The calculation quickly loses accuracy and discrepancies are common with calculators. For the original TI-57 calculator, the result is 9.0047464 (3-digit precision), for the ET-57 calculator, the test result is 8.9999999976 (9-digit precision).

More information on the accuracy of calculators :
http://www.datamath.org/Forensics.htm

## 7. Keyboard

The calculator can work either in direct mode (execution), when the key codes are executed immediately, or in programming mode, when the key codes are only saved in the program, but not executed.

The calculator is controlled by a set of 40 keys arranged in 8 rows and 5 columns. Lines are numbered from top to bottom, in order from 1 to 8.
The columns are numbered from left to right, with numbers from 1 to 5 . It is with this numbering that the key codes are stored in the program.

After pressing the 2nd key, the alternate function of the next key is used, indicated by the column number 6 to 10 (the number 10 is replaced by the number 0 in the code).

When writing the program to memory (using the LRN key), the code of the pressed key is written to the program as a pair of digits, where the first digit represents the row of the key (usually 1 to 9 ) and the second digit represents the column of the key (typically 1 to 5 for the basic function or 6 to 0 for an alternative function).

Numerical key codes from $\quad 0$ to $\quad 9$ are not stored in the program using the key coordinate, but as a decimal value from 00 to 09.

Note: In the text of the manual, the names of the keys are given without any second prefix which may be necessary to invoke the function of the key. For example. the button code Rand (random number) is called by pressing the 2nd and 3 keys.

## 8. On-screen indicators

The LCD display contains 2 lines of 16 alphanumeric characters.
The first line is used to display the indicators, the second line to display the number entered and the result of the operation.


## Deg/Rad/Grd :

indication of the angle unit in degrees, radians or gradians.
$360^{\circ}=2 * \mathrm{PI}$ radians $=400$ gradians .

The angle measurement unit can be changed with the keys Deg, | Rad | or Grad |
| :--- | :--- |

## Fix 0 à Fix 8 :

indicates the selected rounding of numbers from 0 to 8 decimal places. It is set with |  | the keys | Fix | 0 | to |
| :--- | :--- | :--- | :--- | :--- |
|  |  |  |  |  |

 rounding of the displayed result. In this case, the rounding is not indicated on the display (it is replaced by spaces).

## EE :

indicates exponent mode.
After pressing EE , the number is displayed in scientific, mantissa and exponent form.

The mode can be canceled by pressing CLR or | INV | EE |
| :--- | :--- | If exponent mode is off, nothing is shown on the screen..

## 2nd :

indicates that you pressed the alternate function key 2nd
If a key is pressed after pressing 2nd, its alternate function (displayed in the second row of the keyboard) will be executed instead of its base function.
If the key 2 nd is not pressed, or if it is pressed twice, the alternative function is not active, the basic button function is executed.
The basic state is not indicated on the display (spaces are displayed at the position).

## INV :

indicates that you have pressed the key
INV activating the inversion function.

## Opération :

the last position of the 1st line is intended to indicate the active arithmetic operation: + addition, - subtraction, * multiplication, : division, \modulo...

## 9. Number editor

The entered number, together with the results of the calculation, will be displayed on the 2 nd line of the screen. The mantissa is displayed with a maximum of 11 digits.

1 position is reserved for the sign before the mantissa. A '-' will appear here for negative numbers, a space will be left for positive numbers.

The exponent is displayed after the mantissa (if exponent mode is active). The exponent is separated from the mantissa by a + or - sign. The exponent is displayed as 2 digits.

A decimal point is part of the mantissa. In exponent mode in scientific notation (mantissa and exponent), the decimal point always appears after the first digit. If exponent mode is not active, a decimal point is displayed after the units digit.

The key
CE deletes the last character of the mantissa or exponent (depending on where the digits are currently written).

The key
EE starts entering the exponent.
You can return to entering the mantissa by pressing the key $\square$ (period) INV EE

The key EE is also used to start editing the displayed result of the operation. This can be used to remove hidden digits from a number.

Example : round a number to 4 decimal places.

| $\pi$ |  | 3.1415926536 | example of a number with decimals |
| :---: | :---: | :---: | :---: |
| Fix | 4 | 3.1416 | the display is rounded to 4 decimal places |
| EE |  | $3.1416+00$ | start editing, cut hidden digits |
| INV | EE | 3.1416 | turn off exponent mode |
| INV | Fix | 3.1416 | disabling the rounding, the result stays at 3.1416 |

## 10. Numerical expressions

During calculations, the calculator maintains the priority of operations in 3 steps :
(1). ^ power, V square root
(2). * multiplication, : division, $\backslash$ modulo
(3). + addition, - substraction

The calculations are first evaluated at the level (1) power and square root, then (2) multiplication and division, and finally (3) addition and subtraction.

Any number of parentheses can be used in an expression, up to level 7.
After performing the calculation, you can repeat the calculation of the lowest level by pressing the key $=$ again.
Enter a number and press $=$ to repeat the operation. The entered number is used as the first operand of the operation, the second operand remains original.

Note: Calculations are performed internally with 17-digit precision. By storing the result in the X -register, the result is rounded to 15 digits.

Example:

- $3+2=5$
- $4=6$
- $10=12$
- $10+2 * 3 y^{\wedge} \times 4=172$ [similar to $\left.10+\left(2^{*}\left(3^{\wedge} 4\right)\right)=172\right]$


## 11. Registers Addressing

The calculator contains 10 base registers (named $\mathbf{R 0}$ to $\mathbf{R 9}$ ) and 70 additional registers (named R10 to R79), for a total of 80 data registers ( $\mathbf{R 0}$ to R79).

The base registers R0 to $\mathbf{R 9}$ have a mantissa precision of 15 digits. Base registers are used as main working registers. They are addressed by direct addressing, using the instructions :


The base registers are also addressable by the inverse operations:


The instructions INV STO, INV RCL, INV Exc have the same function as the instructions without INV , , but instead of the basic registers RO to R9, they address the additional registers R10 to R19.

Most basic registers have an additional function:
R0 ... number of elements N (Statistics), loop counter Dsz
R1 ... sum of y (Statistics)
R2 $\ldots$ sum of $y^{\wedge} 2$ (Statistics)
R3 ... sum of $x$ (Statistics)
R4 ... sum of $x^{\wedge} 2$ (Statistics)
R5 ... sum of $x^{*} y$ (Statistics)
R6
R7 ... registrer T
R8 ... index register for indirect addressing
R9 ... alternative index register for indirect addressing

The additional data registers $\mathbf{R 1 0}$ to $\mathbf{R 7 9}$ have a precision reduced to 13 digits. By using them, the stored data is shortened by 2 digits.

The additional registers ( $\mathbf{R 1 0}$ to $\mathbf{R 7 9}$ ) cannot be addressed by direct addressing, it is necessary to use indirect addressing :


In indirect addressing, the register number is not part of the instruction, but is read from register R8 (indirect addressing register). Inverses are treated the same way

Indirect addressing operations preceded by
The instructions

have the same function as the same instructions without INV, but, in this case, the alternative index register $\mathbf{R 9}$ is used instead of the index register R8.

Note: The base registers $\mathbf{R 0}$ to $\mathbf{R 9}$ can also be addressed by indirect addressing.

Example, reverse order of register contents :

1) Fill registers R10 to R79 with numbers 0 to 69

switch to program space 1 (and reset pointer)
activate programming mode
label of subroutine 1 (filling registers)
register counter preparation (70 registers)
prepare index register - 1 (pointer to R10-1)
reset $\mathbf{X}$ register
loop start label
increment $\mathbf{R 8}$ (index register)
stores the value of X in the register indexed by $\mathbf{R 8}$
incrementing the $\mathbf{X}$-register
decrements $\mathbf{R 0}$ and skips the next instruction if $\mathbf{R 0}=0$
continue the loop if $\mathbf{R O}$ is not yet equal to 0
end of program
2) Inversion of register contents (R10<->R79, R11<->R78, ...)

3) Display of the contents of registers R10 to R79

label of subroutine 3 (display registers) register counter preparation ( 70 registers)
prepare index register - 1 (pointer to R10-1)
loop start label
increment $\mathbf{R 8}$ (first index register)
read the value of the register indexed by register R8
pause to display value
decrements $\mathbf{R 0}$ and skips the next instruction if $\mathbf{R 0}=0$
continue the loop if $\mathbf{R O}$ is not yet equal to 0
end of program
4) Program testing

exit programming mode
fill registers R10 to R79 with number 0 to 69
display contents of register R19 (9)
check the contents of the registers: the numbers 0 to 69 are displayed
inversion of register contents
display contents of register R19 (60)
check the contents of the registers: the numbers 69 to 0 are displayed

## 12. Programming

Writing a sequence of keystrokes to program memory is called a program. The program turns the calculator into a powerful tool.

Program memory consists of 10 independent program areas, switched by the instruction | Pgm |  |
| :--- | :--- |
| with parameters | 0 |
| to | 9 |

Each program area contains 50 program steps, so a total of 500 program steps are available.
10 labels Lbا, numbered from 0 to $\quad 9$ can be used in each program space. Subroutines can be called or jumps made between program spaces by using the instruction in the program, this instruction does not change program space permanently, but only for an GTO or SBRFommand.

The programs are stored in the processor's EEPROM memory, the contents of which are retained even after the calculator's power supply has been disconnected.

The programming mode is started with the key
The content of the program is displayed on two lines of the display. The bottom line from the left indicates the current program space (Pgm0 to Pgm9), followed by the current pointer in the program, i.e. address 00 to 49.
The address is followed by the numeric code of the instruction.
This instruction code consists of 2 digits. The first digit represents the row with the keys 1 to 8 , the second digit is the column with the keys 1 to 5 or, for the alternative function, the column 6 to 0 . The numeric keys are displayed with the code 00 to 09.
The instruction code can be followed by a parameter from 0 to 9 . The instruction code can also be preceded by the minus sign '-' signifying the inverse functior inv
The top line displays the "text" format of the instruction.


## Keys useful for programming :

SST (Single Step) Increments the program pointer by 1 ("next step"). The SST key can also be used in normal mode (run). In this mode, after pressing SST, the code of the current instruction is executed and the program pointer is positioned on the next step.

BST (Back Step) Decrement the program pointer by 1 ("previous step").

R/S (Run/Stop)
(Delete) Deletes the instruction at the current position of the program and "moves up" the next part of the program.
Inserts an empty instruction (Nop) at the current position of the program and shifts the rest of the program. "hoves up" the next part or the program.
Exits program edit mode and returns the calculator to run mode.
The GTO instruction is normally used to move the program pointer to
the specified label from 0 to 9 . In the "programming" mode, the instruction cannot be used to move the pointer, because the corresponding code would be stored in the program. He must therefore exit programming mode by pressing LRN, make a jump GTO to the specified label 0 to 9 and return to programming mode by pressing

In addition to jumping to a label, GTO allows you to jump to an absolute address in the program. The jump is made by pressing INV GTO, followed by the 2 digits of the address 00 to 49. The jump to absolute address instruction cannot be stored in the program, it is only used to move the pointer during programming and can therefore be entered at the both in execution and in programming.

Note: Jumping to an absolute address is done in a different way (with a different key sequence) on the ET-57 and the original TI57. On the original TI-57, the GTO key was pressed first, then the INV key, and finally the 2-digit address. For the ET-57, you must first press INV, then GTO and finally the 2 digits of the address.

Similar to GTO, cannot be used directly in program mode, but can be used in run mode to return the program pointer to address 00 in the current program space.

Starts the program or stops the program (used in run mode).

## 13. External Devices and Ports



The ET-57 calculator allows connection of an external device using the ISP connector, which is otherwise used to program the calculator's processor. Communication takes place via the SPI protocol. The ISP connector is an 8-pin KONPC-SPK-8 connector with the following pin assignment:

- 1 SCK (serial clock, transmitted by computer)
- 2 MISO (calculator data input, device data output)
- 3 MOSI (calculator data output, in-device data input)
- 4 orientation key, pin missing, blinded in connector so it can't be inserted
- 5 /RESET (processor reset during ISP programming)
- 6 GND (ground, OV)
- 7 VCC (power supply, +5V)
- 8 unused, connected to +5 V in calculator, but in future it may not be used or may be used for SS signal

The connection cable connects the same pins both in the calculator and in the device (no signal crossing).
Note: The SS signal on the slave side must be connected to GND.

The device can be controlled using a 256 -byte addressable port network. A negative number -1 to -256 representing the port address 0 to 255 is stored in the $\mathbf{R 8}$ register of the computer. The STO* instruction sends the number 0 to 255 to the selected port. Conversely, the RCL* instruction reads the value of the selected port as a number between 0 and 255.


Similarly, the INV STO* and INV RCL* instructions can be used, in which the R9 register with the port address is used instead of the R8 register. Instructions other than STO* and RCL* do not allow access to device ports.

If the device is not connected or in another case of a communication error, when using the STO* and RCL* instructions, the program will stop and indicate an error (flashing 'E'). For INV STO* and INV RCL* instructions, the communication error is ignored, the program does not indicate the error and continues to run. Typically, when debugging the program, the STO* and RCL* instructions are used first to ensure that communication problems are reported. After debugging the program, instructions with INV are used to ensure that the program will work without interruption for a long time, even in the event of short-term equipment failures.

Communication takes place using the SPI communication protocol, with a clock frequency of 250 kHz . The ECU acts as a master (control unit), the external device is a slave (subordinate unit). The master (computer) sends serial data on the MOSI line, from the high bit to the low bit. It sends a clock signal to the SCK line, with data sampling on the rising edge.

At the same time, the slave (device) returns data on the MISO line. The transfer of one byte ( 8 bits) takes $32 \mu \mathrm{~s}$. The master adds a 10 us delay after sending each byte so that the slave has time to evaluate the received byte.

The synchronization of the communication between master and slave is not controlled by the SS signal, but by software, by resetting the reception on the slave side. At the start of each transmission, the master sends synchronization byte $0 \times 53$ (the letter ' S ', at bit level 01010011 b ). If the transfer is not synchronized, the data on the slave side is shifted and the slave receives a value other than $0 \times 53$. In such a case, the slave sends byte $0 \times 55$ as an indication of a synchronization error, resets the connection and after a delay of 50 us initiates a new connection. If the slave receives the correct synchronization byte $0 \times 53$, it responds with the same value of $0 \times 53$ and continues communication.

The master sends synchronization bytes $0 \times 53$ several times. If it receives a correct $0 \times 53$ response from the slave, it continues communication. If it receives a byte of $0 x f f$ or $0 \times 00$, it treats it as a device not connected flag and aborts communication with an error indication. If there are other responses, it adds a delay of 100 us and retries the synchronization attempt.

After a successful synchronization, the master continues by sending the command $0 \times 52$ (letter 'R') to read the port from the device or $0 \times 57$ (letter 'W') to write the port to the device. After the command, the master sends a byte with the port address from 0 to 255. After sending the address, the master sends the third byte of the command - data. In the case of a write to the port, it will send data 0 to 255 to write to the port. In the case of a read from the port, the master sends a $0 \times F F$ byte, while the slave sends a byte, it responds with a byte of the data read from the port.

In all other cases, when the slave byte is not specified, the slave responds by repeating the byte received from the master (echo).

## Example of communication (master/slave) :

- Master writes byte $0 \times 24$ to port $0 \times 01$

0x53 / 0x ?? ...master sends 5x SYNC commands for synchronization, response from slave is initially undefined, it is ignored $0 \times 53$ / $0 \times 53$...the slave responds correctly with $0 \times 53$, but the master ignores the response for now, as it may be the rest of the previous communication
$0 \times 53$ / 0x53
$0 \times 53 / 0 \times 53$
$0 \times 53$ / $0 \times 53$...master detects correct response $0 \times 53$, continue
$0 \times 57 / 0 \times 53 \ldots$ master sends command to write $0 \times 57$, slave keeps echoing
$0 \times 01 / 0 \times 57$... the master sends port address $0 \times 01$, the slave has detected a write command, sends the echo of the previous byte and reads the address
$0 \times 24 / 0 \times 01$...the master sends data $0 \times 24$ to be written to the port

- Master rereads data from port 0x01
$0 \times 53 / 0 \times 01 \ldots$ master sends $5 \times$ SYNC commands again for synchronization
$0 \times 530 \times 530 \times 530 \times 53 / 0 \times 530 \times 530 \times 530 \times 53 \ldots$ connected slave
$0 \times 52 / 0 \times 53 \ldots$ the master sends a command to read $0 \times 52$
$0 \times 01$ / 0x52 ... master sends port address 0x01, slave prepares port data for sending $0 \times F F / 0 \times 24 \ldots$ master sends $0 \times F F$ and reads slave data $0 \times 24$


## Example source code to handle Slave communication :

```
u8 SPIData[256]; // SPI slave data
u8 SPIInx; // index of SPI command
u8 SPICmd; // 1st byte - SPI command
u8 SPIAddr; // 2nd byte - SPI address
#define SPICMD_SYNC 
ISR(SPI_STC_vect) // SPI interrupt
{
    u8 d = SPDR; // read data byte
    if (SPIInx == 0) // receive command
    {
    // check known commands
    if ( (d != SPICMD_SYNC) &&
        (d!= SPICMD_READ) &&
        (d != SPICMD_WRITE))
    {
        // error, try to re-synchronize
        SPDR = SPICMD_ERR; // report error to master
        SPI_Term(); // terminate SPI
        _delay_us(50); // short delay 50 us
        \overline{SPI_Slavelnit(); // re-initialize SPI}
        return;
    }
    // shift to next byte of the command
        if (d != SPICMD_SYNC)
        {
        SPICmd = d;
        SPIInx = 1; // next index = address
    }
    }
    else if (SPIlnx == 1) // receive address
    {
    SPIAddr = d; // save address
    SPIInx = 2; // next index = data
    // read data
    if (SPICmd == SPICMD_READ) SPDR = SPIData[d];
    }
    else // receive data
    {
    // next index = command
    SPIInx = 0;
    // write data
    if (SPICmd == SPICMD_WRITE) SPIData[SPIAddr] = d;
    }
}
```


## 14. Keys and instructions

Each instruction has a BCD program code, a title and a sequence of presses on one or more keys to express it.
$00 \ldots 09 \square 0 \ldots 9$ - Basic digits
Base digits are used to enter digits in the range 0 to 9 . They are used to enter the mantissa of a number, enter the exponent, memory register number, tag number, and others.

The numbers are stored in the program with the code 00 to 09.

## 10 2nd CLR OFF - Stop calculator (ET-57B)

The $\mathbf{2 n d}$ CLR (OFF) sequence is used to turn off the calculator.
The calculator can be turned back on by pressing the CLR key alone.

By specifying the INV prefix before the OFF statement, the contrast of the LCD display can be adjusted.
The instruction requires a numeric code from 0 to 9 as a parameter.
0 sets the lowest display contrast (light font on light background), 9 sets the highest display contrast (dark font on dark background).

The OFF and INV OFF functions are only available for the ET-57B variant of the calculator.
The ET-57 calculator cannot be turned off with a button, nor can the contrast of the display be controlled.

## 11 2nd 2nd - Alternate function

The $\mathbf{2 n d}$ key is used to change the meaning of the next key to an alternate function. After pressing $\mathbf{2 n d}$, the alternate function of the next button is then executed.
A second press on $\mathbf{2 n d}$ returns to the basic functions. (cancels the first press on $\mathbf{2 n d}$ ).

The code for the $\mathbf{2 n d}$ key (11) is not saved in the program, it is the alternative code for the next key which is then saved.

## Example:

$2 \ln x$
... calculate the natural logarithm of the number 2 [0.6931...]
2 2nd Inx ... decimal logarithm of the number 2 (log instruction) [0.3010...]

## 12 INV INV - Inverse of a function

The INV key, pressed before another key, will cause that other key to have its function reversed.
In some special cases, INV will not cause the inverse of the following function but an additional alternative function.
A second press on INV returns to the basic functions. (cancels the first press on INV).
The INV button code is not saved in the program. It is stored as an instruction indicator with the minus sign (-) before the instruction code.
Some instructions do not accept the INV prefix, which is then ignored and the instruction code is stored without the prefix in the program.

## Example:

10 sin ... calculate the sine of 10 [ $0,1736 \ldots]$
0.1 2 INV sin ... calculates the arcsine of 0.12 [0.3464...]

## 13 Inx Inx - Natural logarithm and exponent

Inx calculates the natural logarithm of the displayed number. This natural logarithm uses Euler's constant as its base with the value 2.718281828459. If the INV button is pressed first, the inverse function, the natural exponent, is executed.
The argument of the Inx function must be a non-zero positive number. In the case of zero, the display will flash with the value -9.9999+99, as an error indication.
For a negative number, the absolute value of the number is calculated and the display flashes again with an error indication.

The argument to the INV Inx function can be a positive or negative number, ranging from approximately -227 to +227 . A number outside this range will result in data overflow and indicate an error.

## Example:

$5 \operatorname{lnx}$... calculates the natural logarithm of 5 [1.6094...]
5 INV Inx ... calculates the natural exponent of 5 [148.413...]

## 14 CE CE - Error correction

CE can be used to cancel the 'E' error indication, manifested by flashing of the display. When entering a number, the last character entered is deleted by pressing the CE key.

In scientific notation, if the mantissa is being entered, the last character of the mantissa is removed. If the exponent is being entered, the last character of the exponent is deleted. If an exponent with a value of 0 is removed, the exponent is canceled and the input reverts to the mantissa.

## 15 CLR CLR - Clearing the display

CLR performs several initialization operations.
It resets started arithmetic operations, resets error indication, turns off EE exponent mode, resets the X-register, and starts editing a new number with a default value of 0 .
The CLR key does not reset the $\mathbf{T}$ register or the data registers. In the ET-57B calculator variant, the CLR key is used to turn the calculator on (or off).

## 18 2nd Inx log-Decimal logarithm and exponent

log calculates the decimal logarithm of the displayed number.
The decimal logarithm uses the number 10 as its base. If the INV key is pressed first, the inverse function, the decimal exponent, is executed.
The argument to the log function must be a non-zero positive number. In the case of zero, the display will flash with the value -9.9999+99, as an error indication.
For a negative number, the absolute value of the number is calculated and the display flashes again with an error indication.
The argument of the INV log function can be both a positive number and a negative number, ranging from -99 to +99 . A number outside this range will result in data overflow and an error indication.

## Example:

5 log ... calculates the decimal logarithm of 5 [.69897...]
5 INV log ... calculates the decimal exponent of 5 [100000]
19 2nd $C E$ C.t-Clear register $T$
The C.t key can be used to clear the $\mathbf{T}$ register (i.e. R7 register).

> Entering the INV prefix before the key C.t clears all registers R0 to R79 (including the $\mathbf{T}$ register).
20 2nd 1/x tan - Tangent

The tan function calculates the tangent of an angle. The angle is entered in the units defined by the Deg, Rad or Grad switches.
Typing the INV prefix before the tan statement will perform the opposite function (arctangent).
The result is an angle in the currently defined angular measurement.

## Example:

50 tan ... calculates the tangent of 50 [1.19175...]
50 INV tan ... calculates the arctangent of 50 [88.85423...]
21 LRN LRN - Programming

LRN enables or disables programming mode.

## $22 \quad x<>t$ - Exchange of $X$ and $T$ registers

With the $\mathbf{x}<>\mathbf{t}$ key, it is possible to switch between the $\mathbf{X}$ and $\mathbf{T}$ registers.
The $\mathbf{X}$-register is the working register and also the display content.
Register $\mathbf{T}$ is an auxiliary (temporary) register, corresponds to register R07. It is used to compare numbers and to convert polar and Cartesian coordinates.
The $\mathbf{X}$ register is reset by the CLR key.
The $\mathbf{T}$ register is reset by the C.t key.
$23 \quad x^{2} \quad x^{\wedge} 2$ - Square of a number
The $\mathbf{x}$ ^2 function calculates the square of a number, or the multiple of a number by itself.
$24 \sqrt{x} \quad \sqrt{x}$ - Square root of a number
$\mathbf{V} \mathbf{X}$ calculates the square root of a number. The number must not be negative. If a negative number is calculated, the square root of the absolute value of the number is calculated and the error indication ' $\mathbf{E}$ ' is activated (display flashes).

## $25 \quad 1 / \mathrm{x} \quad 1 / \mathrm{x}$ - Inverse of a number

The $\mathbf{1} / \mathbf{x}$ function calculates the inverse of a number.
If the number is zero, the value $9.9999+99$ is displayed and the error indication ' $\mathbf{E}$ ' is activated (display flashes).
This application of $\mathbf{0} \mathbf{1} / \mathbf{x}$ is often used in programs to activate error indication and to signal abnormal operation of the program.

## 26 2nd LRN D.MS - Conversion of minutes and seconds

The D.MS instruction is used to convert time expressed in hours/mins/seconds or angle expressed in degrees/minutes/seconds to a decimal number. The original number HH.MMSS or DD.MMSS, is entered with the number of hours, or degrees, in the integer position, then with the number of minutes in the first two decimal places and finally with the number of seconds in the next two decimal places.
The result of the function is a decimal number representing the number of hours, or degrees, expressed as a decimal number DD.DDDD.
By specifying the INV prefix before the D.MS instruction, the reverse operation is performed - time or angle expressed using a decimal number is converted to hours/ minures/seconds or degrees/minutes/seconds .
The decimal number DD.DDDD representing hours or degrees will be returned as HH.MMSS or DD.MMSS, with the number of hours, or degrees, in the integer part, and the number of minutes in the first two decimal places followed by the number of seconds in the next two decimal places. If the result is not an integer number of seconds, the decimal seconds are padded with additional decimal digits.

## Example:

12 . 302 3 D.MS ... conversion to decimals [12.50638...]

+ 3.4512 D.MS ... conversion to decimals [3.75333...]
= INV D.MS ... resulting time [16.1535]
Sum of time:
12 hours, 30 minutes and 23 seconds
+3 hours, 45 minutes and 12 seconds
$=16$ hours, 15 minutes and 35 seconds


## 27 2nd $x$ x:t $\quad$ P->R - Conversion polar / cartesian

$\mathbf{P}->\mathbf{R}$ converts the coordinates of the polar expression (radius/angle) into Cartesian coordinates (abscissa and ordinate).
Before the operation, the $\mathbf{T}$ register (i.e. auxiliary register R7) contains the radius and the $\mathbf{X}$-register (content of the display) contains the angle. The angle is given in the selected angular measurement (Deg, Rad or Grad).
After the operation, the $\mathbf{T}$ register (auxiliary register R7) contains the abscissa X , the $\mathbf{X}$ register (display content) contains the ordinate Y .
By specifying the INV prefix before the $\mathbf{P}-\mathbf{P}$ instruction, the inverse operation is performed, the conversion from Cartesian coordinates to polar.
Before the operation, the $\mathbf{T}$ register contains the abscissa $X$, the $\mathbf{X}$ register (display) contains the ordinate Y .
After the operation, the $\mathbf{T}$ register contains the radius and the $\mathbf{X}$-register (display) contains the angle. The angle is given in the selected angular measurement.

## Example :

$\mathbf{1 0} \mathbf{0}<>\mathbf{t} \ldots$ enter radius 10 in register $T$
30 ... entry of the $30^{\circ}$ angle in the X-register
$\mathbf{P}->\mathbf{R} . .$. conversion from polar to Cartesian coordinates. $Y=5$
$\mathbf{x}<>\mathbf{t} . .$. exchange $X$ and $T$ displays coordinates $X=8.6602 \ldots$
8.6602... $\mathbf{x}<>\mathbf{t}$... $X$ abscissa input

5 ... Y ordinate input
INV $\mathbf{P}$->R... Cartesian to polar conversion, angle $=30^{\circ}$
$\mathbf{x}<>\mathbf{t} .$. swap $\mathbf{X}$ and $\mathbf{T}$, show radius 10

## 28 2nd $x^{2}$ sin-Sine

The sin function calculates the sine of an angle. The angle is entered in the units defined by the Deg, Rad or Grad switches.
Typing the INV prefix before the sin statement will perform the opposite arcsine function. The result is an angle in the defined angular measurement.
The angle calculated by the arcsine function is between $-90^{\circ}$ and $+90^{\circ}$. The input value of the arcsine function must be between -1 and +1 . If it is outside the specified range, the display is limited to the valid range and an "E" error is indicated (display flashes).

## 29 2nd

The cos function calculates the cosine of an angle. The angle is entered in the defined unit Deg, Rad or Grad.
Typing the INV prefix before the cos statement performs the opposite arccosine function. The result is an angle in the defined angular measurement.
The angle calculated by the arccosine function is between $0^{\circ}$ and $+180^{\circ}$. The input value of the arccosine function must be between -1 and +1 . If it is outside the specified range, the display is limited to the valid range and an "E" error is indicated (display flashes).

30 2nd $\mathbf{y s}^{\mathbf{x}}$ PI - Ludolf's number
The pi key is used to enter the constant "Ludolf's number", which has a value of 3.14159265358979.

## 31 SST SST - Advance one step in program

The SST (Single Step) key increments the program address pointer by 1 in programming mode.
In run mode, the program statement, on which the pointer is positioned, is executed, allowing the program to be run step by step for debugging purposes.
Caution : in this case of step by step test of the program if a subroutine is called, the return of the subroutine cannot occur correctly (the calculator does not memorize the return address of the subroutine).

32 STO STO - Store a number in a register
STO (Store) stores the displayed number in data register R0 to R9. A register number from 0 to 9 is entered as an instruction parameter.
The INV prefix before the STO instruction performs a similar function, but instead of registers R0 through R9, the number is stored in registers $\mathbf{R 1 0}$ through R19. Registers R10 to R19 belong to the group of extended registers with a precision reduced to 13 digits. Recording deletes the last 2 digits of the mantissa.

33 RCL RCL - Recall a number from a register
$\mathbf{R C L}$ (Recall) is used to recall a number from data register $\mathbf{R 0}$ to $\mathbf{R 9}$ to the display. A register number from 0 to 9 is entered as an instruction parameter.
Placing the INV prefix before the RCL instruction performs a similar function, but instead of the R0 to $\mathbf{R 9}$ register, the number is read from the $\mathbf{R 1 0}$ to $\mathbf{R 1 9}$ register. Registers R10 to R19 belong to the group of extended registers with a precision reduced to 13 digits. The mantissa is completed by 2 digits 0 at the end.

## 34 SUM SUM - Add and subtract into a register

SUM adds the displayed number ( $\mathbf{X}$ register) to register R0 to R9. A register number from 0 to 9 is entered as an instruction parameter.
By specifying the INV prefix before the SUM instruction, the opposite function is performed - subtracting a number from the data register R0 to R9.

## $35 \quad y^{x} \quad y^{\wedge} x$ - Power and root

The instruction $\mathbf{y}^{\wedge} \mathbf{x}$ raises the number Y (the first operand, in the stack of operations) to the power expressed by another number $X$ (the second operand, the number on the display).
If the INV prefix is pressed first, the inverse operation, the Xth root, is performed. The first operand of $Y$ must be a non-negative number. If this is the lowest level of the expression, the calculation can be repeated for another first operand by pressing $=$ repeatedly.

## Example:

$3 \mathbf{y}^{\wedge} \mathbf{7}$... raise 3 to power 7 [2187]
2187 INV $\mathbf{y}^{\wedge} \mathbf{x} 7$... 7th root of 2187 (2187^(1/7)) [3]

## 36 2nd SST Pause - Delay

The Pause command stops program execution for 0.25 seconds and displays the contents of the register $\mathbf{X}$.

37
2nd
STO Ins - Inserting an empty step in the program
The Ins key, used in programming mode, inserts an empty Nop instruction at the program pointer position. The following steps are shifted downwards.

## 38 2nd RCL Exc - Exchange $\mathbf{X}$ with a register

Exc exchanges the displayed number ( $\mathbf{X}$ register) with the contents of data register $\mathbf{R 0}$ to R9. A register number from 0 to 9 is entered as an instruction parameter.
Placing the INV prefix before the Exc instruction performs a similar function, but instead of using registers R0 through R9, the number is swapped with registers $\mathbf{R 1 0}$ through R19. Registers R10 to R19 belong to the group of extended registers with a precision reduced to 13 digits. When saving, the last 2 digits are removed from the mantissa, and when loading, the mantissa is completed with 2 digits 0 at the end.

Prd is used to multiply the data registers R0 to R9 by the number displayed (register X). A register number from 0 to 9 is entered as an instruction parameter.

By entering the INV prefix before the Prd instruction, the inverse function is performed by dividing the data register $\mathbf{R 0}$ to $\mathbf{R 9}$ by the displayed number.

## $40 \quad$ 2nd $\quad \div \quad$ IxI - Absolute value

The IxI function adjusts the number to the absolute value (removes the negative sign from the number).
If the INV prefix is specified before pressing IxI, the absolute value is not applied but a sign test is performed on the number. If this number is less than 0 , the result of the operation is -1 , if this number is greater than 0 , the result is +1 . If the number is 0,0 remains.

## 41 BST BST - Back step in program

The BST (Back Step) key in programming mode decrements the program address pointer by 1.

## 42 EE EE - Exponent mode

Press EE to activate exponent mode.
If the key is pressed while entering a number, it switches to entering the exponent.
At the same time, the display mode in scientific notation with an exponent is activated.
If the key is pressed outside the entry of a number, the display mode in scientific notation with an exponent is activated and the entry of the exponent of the number is launched. This feature is often used to remove hidden digits from a number, because when you start typing, only the displayed digits are written to the display, not the full exact value of the number.
Press the INV prefix before pressing EE to exit exponent display mode. Another way to exit exponent display mode is to press the CLR key.

## Example:

pi Fix 4 EE INV EE INV Fix ... round PI number to 4 decimal places [3.1416]

## $43 \quad 1$ <br> ( - Left parenthesis

The character ( opens the calculation of part of the expression.
Parentheses can be used up to 7 levels.
$44 \quad$ ) $\quad$ - Right parenthesis
The character ) closes the calculation of part of the expression.

## $45 \quad \div$ <br> : - Divide

The sign : divides the first operand by the second operand. If this is the lowest level of the expression, the calculation can be repeated for another first operand by pressing = repeatedly.
Pressing the INV prefix before pressing : executes the inverse function, i.e. the modulo mod operation which returns the remainder after division. The modulo operation divides the first operand $Y$ (in the stack) by the second operand $X$ (on the display), converts the result to an integer, multiplies the second operand $X$ by it, and subtracts from the first operand $Y$. The result is the remainder after division. The result has the same sign as the first operand.

## Example:

2. 2: 0. 5 = ... divide 2.2 by 0.5 [4.4]
2.2 INV : 0. 5 = ... calculates the remainder of 2,2 divided by $0,5[0,2]$
3. $\mathbf{2}$ +/- INV : $\mathbf{0}$. $\mathbf{5}=\ldots$ calculates the remainder of $-2,2$ divided by $0,5[-0,2]$
4. 2 INV : 0 . 5 +/- = ... calculates the remainder of 2,2 divided by $-0,5[0,2]$
5. $\mathbf{2}+/-$ INV : $\mathbf{0} \cdot \mathbf{5}+/-=\ldots$ calculates the remainder of $-2,2$ divided by $-0,5[-0,2]$

## 46 2nd BST Nop - No operation

The Nop (No Operation) command is an empty command that does not perform any operation. It is only used to fill an unused step in the program.

## 47 2nd EE Del-Delete a program step

The Del (Delete) key, used in programming mode, deletes a step from the current program position. The following steps are then shifted upwards..

## 48

2nd
Fix - Number of decimal places
Using the Fix key, the number displayed on the screen is rounded to the number of decimal places
specified. The number 0 to 8 is entered as a parameter, representing the number of decimals after the decimal point 0 to 8 .
In rounding mode, the number is padded from the right with zeros, up to the specified number of decimal places. Entering the sequence INV Fix or Fix 9 disables rounding. In this case, the number is displayed with full precision and trailing leading zeros are suppressed.
Rounding only affects the display of the number. Internally, the number ( $\mathbf{X}$ register) continues to be stored in full. If it is necessary to actually remove the hidden digits, this can be done using the EE key (see 42 Exponent mode, EE).
The rounding mode set also affects how very small numbers are displayed. If rounding is on and exponent mode is not on, the screen displays zeros for small numbers, even though the valid digits have passed the right edge of the screen. If rounding is not enabled, the calculator will switch to displaying the exponent if the exponent is less than -3.

## 49 2nd $\quad$ ) Int - Integer part

The Int key is used to remove the digits after the decimal point of the number or to reduce the number to an integer.
The function has the same meaning as rounding towards zero.
If the INV prefix is used before the Int command, the inverse function is executed (Frac) by removing the integer part of the number and keeping only the decimal part.

## Example:

2. 3 int ... integer part of 2.3 [2]
3. 3 +/- Int ... integer part of -2.3 [-2]
4. 3 INV Int ... decimal part of 2.3 [0.3]
5. $\mathbf{3}$ +/- INV Int ... decimal part of de -2.3 [-0.3]

## 50 2nd $\quad \mathbf{x}$ Deg-Degrees

The Deg key switches trigonometric function calculations to degrees (a full angle is $360^{\circ}$ ).

## 51 GTO GTO - Go to a label (or address)

GTO allows you to perform an unconditional jump in a program. Its parameter is a numeric code from 0 to 9 corresponding to a label (Lbl) of the program.
By entering the Pgm command in the program before the GTO command, a jump to the label in another program area can be performed.
When the GTO instruction is used in run mode, the program pointer is positioned on the selected label.
By pressing the INV prefix before the GTO instruction, the pointer in the program can be moved to an absolute address, which is entered as a 2-digit numeric code from 00 to 49. This function cannot do part of the program, it is executed immediately, and makes it possible to move the program pointer both in execution mode and in programming mode.
The GTO key has another special function: if you hold it down while the program is running, the display will scroll through the contents of the display ( $\mathbf{X}$ register) on the bottom line, and the address of the step executed on the upper line. However, this tracking slows down the program considerably.

## $55 \quad \mathrm{x} \quad \mathrm{x}$ - Multiply

The $\mathbf{x}$ key is used to multiply a first operand by a second operand. If this is the lowest level of the expression, the calculation can be repeated for another first operand by repeatedly pressing $=$.

## 56

The Dsz instruction is used to execute a program sequence iteratively using a loop according to a number of passes specified in the $\mathbf{R O}$ register.
The Dsz function consists in the fact that it decrements (decreases by 1) the register RO and stops looping as soon as it reaches zero, it ignores the next command and continues the operation at the next step. If zero is not reached (ie the loop has not yet terminated), the command following the Dsz command is executed. Typically, Dsz is followed by the GTO command, which returns to the start of the loop label.

If the INV prefix is given before the Dsz instruction, the opposite direction of the instruction is executed - the next instruction is skipped if the decrement result is not zero. This variant is generally used at the beginning of the loop. When the loop counter reaches zero, the next statement, which is usually a loop statement GTO, is executed,

Dsz handles the RO register and works more precisely as follows : If the value contained in register R0

- is greater than 0 before the operation, the register value is decreased by 1 .
- is less than 0 , the value is increased by 1 .
- is equal to 0 , the value remains unchanged.

If the result of the operation is zero or the operation has crossed the zero boundary, the operation for zero is performed according to the selected function.
Which means that if the decrement/increment result did not reach zero, the loop repeats (the next instruction is executed). With the INV prefix, a jump is performed on the contrary if the result of the operation reaches zero (or exceeds it).

Example (factorial of a number) :


## 57 2nd $\quad 7 \quad$ STO* - Indirect storage of a register

STO* stores the contents of the $\mathbf{X}$ (display) register in a data register in the same way as the STO instruction.
On the other hand, instead of using an instruction parameter as destination register number, the destination register number is contained in register R8.
All data registers R0 to $\mathbf{R 7 9}$ can be addressed indirectly in this way.
If the INV prefix is given before the instruction, the destination register number is contained in the $\mathbf{R 9} 9$ register (alternative index).
Registers R10 to R79 belong to the group of extended registers with a precision reduced to 13 digits.
Saving deletes the last 2 digits of the mantissa.
Entering address -1 to -256 (negative number) in register R8 (or R9) with instruction
STO* (or INV STO*) sends a byte with value 0 to 255 (display number) at port 0 to 255
(depending on the content of register R8, R9) to the connected external device. (See External Devices and Ports).
This function cannot be used with the ET-57B calculator variant.

## 58 2nd 8 RCL* - Indirect recall of a register

RCL* recalls a number from a data register in the same way as the RCL instruction. On the other hand, instead of using an instruction parameter as the number of the original register of the number to be recovered, the number of the original register is contained in the register R8.
All registers from R0 to R79 can be addressed indirectly in this way.
If the INV prefix is given before the instruction, the original register number is contained in the $\mathbf{R 9}$ register (alternative index).
Registers R10 to R79 belong to the group of extended registers with a precision reduced to 13 digits.
The mantissa is completed by 2 digits 0 at the end.
Entering the address -1 to -256 (negative number) in the R8 (or R9) register with the RCL* (or INV RCL*) instruction, reads a byte with the value 0 to 255 from port 0 to 255 (depending on the content of register R8, R9) of a connected external device. (See External Devices and Ports).
This function cannot be used with the ET-57B calculator variant.

## 59 2nd 9 SUM* - Indirect add into a register

The SUM* instruction adds (or subtracts with INV) a number to the destination register in the same way as the SUM instruction, only instead of the instruction parameter, the destination register number is held in the $\mathbf{R 8}$ register.
Registers R10 to $\mathbf{R 7 9}$ belong to the group of extended registers with a precision reduced to 13 digits.
The mantissa is completed by 2 digits 0 at the end.

## 60 2nd - Rad - Radians

The Rad key toggles trigonometric function calculations in radians (a full angle is $2 * \mathrm{pi}$ rad).

## 61 SBR <br> SBR - Subroutine call

The SBR (Subroutine) key is used to call a subroutine using as a parameter the numeric code from 0 to 9 of the called label.
By specifying the Pgm command in the program before the SBR command, a subroutine from another program space is called.
If the SBR instruction is used in run mode, the subroutine is executed immediately.
When calling a subroutine, the address of the instruction following the SBR instruction code is first stored in the address stack. The address stack has a capacity limited to 7 subroutines.
The subroutine ends with the INV SBR instruction which ensures the return of the subroutine to the calling program thanks to the original address which is taken from the address stack.
If the subroutine was launched from another program space, control returns to the original program space. If the subroutine was started from the keyboard, execution stops.

## 65 <br> - <br> - - Substraction

The minus sign (-) is used to subtract the operand entered after the sign from the operand entered before the sign. If this is the lowest level of the expression, the calculation can be repeated for another first operand by pressing $=$ repeatedly.
Entering the prefix INV before the minus sign (-) deactivates debug mode (display of the mantissa of the number). Debug mode is activated by the INV + instruction.

## 66 <br> 2nd <br> SBR <br> $\mathbf{x}=\mathrm{t}$ - Equality test

The instruction $\mathbf{x = t}$ makes it possible to compare the register $\mathbf{X}$ (content of display) with the auxiliary register $\mathbf{T}$ (loaded by the key $\mathbf{x}<>\mathbf{t}$, corresponds to the register $\mathbf{R 7}$ ). If the registers match, the next instruction is executed. Otherwise, the program jumps to the next instruction.
If the INV prefix is specified before the $\mathbf{x}=\mathbf{t}$ code, the inverse function is executed - the execution of the following command if the $\mathbf{X}$ register is different from the $\mathbf{T}$ register.

## 67 2nd 4 Inc* - Register Increment/Decrement

The Inc* instruction allows to increment/decrement the content of a data register in the same way as the Inc instruction, only instead of the instruction parameter specifying the register number, this register number is contained in the $\mathbf{R 8}$ register.
By placing the INV prefix before the Inc* instruction, instead of the increment of 1 of the target register, the decrement of -1 is performed.

## 68

The Exc* instruction is used to exchange the displayed number with the contents of a data register similar to the Exc instruction.
On the other hand, instead of using an instruction parameter as the number of the register containing the value to be exchanged, the number of this register is contained in the register R8.
All data registers R0 to $\mathbf{R 7 9}$ can be addressed indirectly in this way.
If the INV prefix is given before the instruction Exc*, the register number is taken from the data register $\mathbf{R 9}$ (alternative index).

## 69 2nd 6 Prd* - Multiply in an indirect register

The Prd* instruction is used to multiply or divide (with the INV prefix) the contents of a data register by the entered number in the same way as the Prd instruction.
On the other hand, instead of using an instruction parameter as the number of the register containing the value to be multiplied, the number of this register is contained in the register $\mathbf{R 8}$.
All registers from R0 to $\mathbf{R 7 9}$ can be indirectly addressed in this way.

70 2nd $\quad+\quad$ Grd - Gradians
The Grd key switches trigonometric function calculations to grads (a full angle is 400 gon).

## 71 RST RST - Reset step address

The RST key is used to reset the program pointer, ie to reset the pointer to 0 (not 00). The selected program area remains unchanged.

## $75 \quad+\quad+$ - Addition

The plus sign (+) adds the operand entered after the sign to the operand entered before the sign. If this is the lowest level of the expression, the calculation can be repeated for another first operand by pressing = repeatedly.
Entering the INV prefix before the plus sign (+) activates debug mode (displays the mantissa of the number). Debug mode can be disabled by the INV - instruction.

The instruction $\mathbf{x}>=\mathbf{t}$ makes it possible to compare the register $\mathbf{X}$ (content of display) with the auxiliary register $\mathbf{T}$ (loaded by the key $\mathbf{x}<>\mathbf{t}$, corresponds to the register $\mathbf{R 7}$ ). If register $\mathbf{X}$ is greater than or equal to register $\mathbf{T}$, the instruction following the instruction $\mathbf{x}>=\mathbf{t}$ is executed. Otherwise, the next command is ignored.
If the INV prefix is specified before the $\mathbf{x}>=\mathbf{t}$ code, the inverse function is executed the execution of the following command if the $\mathbf{X}$ register is smaller than the $\mathbf{T}$ register.

## 77 2nd 1 Inc. - Increment/Decrement a Register

The Inc instruction increments (increases by 1) the content of a data register R0 to R9, whose number 0 to 9 is given as an instruction parameter. If the INV prefix is given before the Inc instruction, the reverse operation is performed - decrement the register (decrease by 1 ).

## 78 2nd $\quad 2 \quad$ Pgm - Program space selection

A program area can be selected with the Pgm key. The program area is selected by entering the number 0 to 9 as a parameter of the $\mathbf{P g m}$ instruction.
There are a total of 10 independent program areas available in the calculator, marked with numbers from 0 to 9 .
Each program area has 50 program steps, i.e. a total of 500 program steps in all.
When switching the program area in run mode (from the keyboard), the program pointer is simultaneously reset to the start of the newly selected program area (step 00).

Entering the Pgm command into a program does not change the program space permanently, only temporarily for a later GTO or SBR instruction.
In this way, subroutines can be called or jumps between program areas can be made.
The GTO and SBR instructions do not have to immediately follow the Pgm instruction.

## 79 2nd 3 Rand-Random number generator

The Rand function calculates a random number greater than or equal to 0 and less than 1.

The LCG (Linear Congruential Generator) and the formula
Rand $=($ Seed $-($ Seed $* 214013+2531011) \bmod 4294967296) / 4294967296$
are used to calculate the random number.
The generator seed has a range of 32 bits. The generated number is converted to a float by dividing by $2^{\wedge} 32$. This ensures that the resulting random number is between 0 and 1 , including zero but excluding the value 1 .
The random number generator keeps counting each time it is used, which ensures that the sequence of numbers generated does not repeat (more precisely - the repeat interval is very large, $2^{\wedge} 32$ numbers). Each time the calculator is turned on, the generator seed is read from the EEPROM and a new value is stored. This ensures that generated sequences do not repeat after the calculator is powered on.

## Example:



The test can be completed with a counting test of the number of outputs of each number ( 1 to 6 ) and the counting of the number of throws per second.

## Continued Example :

LRN


After 10 minutes of testing, the $\mathbf{R 1}$ to $\mathbf{R 6}$ registers contain roughly similar numbers (similar case numbers), the R0 and $\mathbf{R 7}$ registers must contain 0.
(for example: 0, 2762, 2727, 2834, 2701, 2671, 2763, 0, which corresponds to the hypothesis of a generation speed of 27 dice rolls per second and a fairly homogeneous distribution between 1 and 6.)

## 80 2nd $=$ Var - Scatter

The Var statement calculates the variance of the ' $x$ ' and ' $y$ ' values entered using the statistical function Stat. Pressing Var displays the variance of the ' $y$ ' values, and using INV before the Var statement displays the variance of the ' $x$ ' values.
The variance is calculated by the formula :

$$
\operatorname{var}=\operatorname{sum}\left(y^{\wedge} 2\right) / N-(\operatorname{sum}(y) / N)^{\wedge} 2
$$

The square root of the variance gives the standard deviation ' $s$ '.

## 81 R/S R/S - Program start and stop

The R/S key can be used to start or stop a running program.
On startup, the program begins to run from the current program pointer (the current address can be found by switching to LRN programming mode).
After stopping, the program may not always be able to continue running - the subroutine's return address may be lost.
$83 \quad$ - . - Decimal point
The dot (.) is the separator for whole digits and decimal digits in a number.
In scientific notation, if this key is pressed while entering the exponent of a number, editing reverts to entering the mantissa of the number.

## $84 \quad+/-\quad$ - Change of sign

The +/- key changes the sign of the number on the display.
Using it while typing the exponent of a number in scientific notation, changes the sign of that exponent.

## $85==$ - Perform the calculation

The $=$ sign is used to close open arithmetic operations and to perform calculations. By repeatedly pressing the $=$ key, the last operation performed at the lowest level can be repeated. The first operand is the displayed number, the second operand is the number entered during the operation as the second operand (or second result of the intermediate calculation).
Caution: Some original TI-57 programs, for which repetitive operations are not allowed, use the = key more than once to cause an error. When importing a program, it may be necessary to check and solve this case.

## Example:

| $5 \times 6=$ | $[30]$ |
| :--- | :--- |
| $7=$ | $[42]$ |$\quad \ldots 5 \times 6=304 \times 6=42$ the second operand (6) is reused

## 86 2nd R/S Lbl - Labels

The Lbl instruction can be used to mark the beginning of a sequence in the program like a label.
In each program area, 10 labels can be used, denoted Lbl $\mathbf{0}$ to Lbl 9. The label number is specified as numeric parameter 0 to 9 of the $\mathbf{L b I}$ instruction.
You can jump to the program location marked with a label using the GTO jump instruction or the SBR subroutine call instruction.
With the use of the Pgm program space select statement, jumps and subroutine calls can also be made between program spaces.

## 87 2nd 0 x! - Factorial

The $\mathbf{x}$ ! key is used to calculate the factorial. The factorial of a number is obtained by multiplying the successive values $1,2,3, \ldots$ up to the specified number. The number entered is an integer between 1 and 69.
(69! =
17112245242814131137246833888127283909227054489352036939364804092325
7279754140647424000000000000000 [99 digits])

## Example:

6 x! ... factorial of the number $6[6!=1 * 2 * 3 * 4 * 5 * 6=720$ ]

## 88 2nd - Stat - Statistics

The Stat instruction is used to enter data that can be used for statistical calculations (mean, variance).
The instruction uses data registers $\mathbf{R 0}$ through $\mathbf{R 5}$ to store the intermediate calculation. Before use, it is advisable to first reset the registers with the INV C.t command, which resets all data registers R0 to R79.

Use of data registers :

- R0 ... number of elements N
- R1 ... the sum of $y$ - R3 ... the sum of $x$
- R2 ... the sum of $y^{\wedge} 2$ - R4 ... the sum of $x^{\wedge} 2$
- R5 $\ldots$ the sum of $x^{*} y$
and $\mathbf{R 7}$... T register

When entering statistical data in pairs ( $x, y$ ), the value ' $x$ ' is entered first and by pressing $\mathbf{x}<>\mathbf{t}$ it is transferred to the $\mathbf{T}$ register (register $\mathbf{R 7}$ ).
Then the ' $y$ ' value is entered and by pressing Stat the ' $x$ ' and ' $y$ ' values are saved.
The display (in the $\mathbf{X}$ register) will show the number of ' $n$ ' elements inserted so far. The content of the $\mathbf{T}$ register (the value of ' $x$ ') is increased by 1 with the Stat instruction, because if the values of ' $x$ ' must increment by 1 , it is not necessary to insert them, it is enough to insert the initial value of ' $x$ ' into the $\mathbf{T}$ register, then write only the ' $y$ ' values. If it is not necessary to evaluate pairs of values ( $x, y$ ), just enter the value ' $y$ '.
If the INV prefix is used before the Stat instruction, the entered value will be subtracted. This is how you can correct a wrong value - enter the ' $x$ ' value of the wrong data, press $\mathbf{x}<>\mathbf{t}$, enter the ' $y$ ' value of the wrong data and press INV Stat to delete the wrong data. The content of register $\mathbf{T}$ (with the value 'x') is then decremented by 1.
Then the entry of new correct data can be continued. If it is not necessary to evaluate pairs of values ( $x, y$ ), it is sufficient to enter only the value ' $y$ ' of the erroneous data.

## Example:

| INV | C.t |  |  | ...initializing data registers |
| :---: | :---: | :---: | :---: | :---: |
| 9 | 6 | Stat | [1] | ... 1st data 96 |
| 8 | 1 | Stat | [2] | ... 2nd data 81 |
| 9 | 7 | Stat | [3] | ... 3rd incorrect data |
| 9 | 7 | Stat | [2] | ... cancellation of the 3rd data |
| 8 | 7 | Stat | [3] | ... 3rd corrected data 87 |
| 7 | 0 | Stat | [4] | ... 4th data 70 |
| 9 | 3 | Stat | [5] | ... 5th data 93 |
| 7 | 7 | Stat | [6] | ... 6th data 77 |
| Mean |  |  | [84] | ... average of the entered values |
| Var |  |  | [81,333...] | ... Deviation |
| $\sqrt{x}$ |  |  | [9.0185...] | ... standard deviation |
| RCL | 1 |  | [504] | ... sum of all values |

## 89 2nd +/- Mean - Mean

The Mean statement calculates the average of the ' $x$ ' and ' $y$ ' values entered using the statistical function Stat.
After pressing Mean, the display shows the average of the 'y' values.
Typing the INV prefix before the Mean statement calculates the average of the ' $x$ ' values.
15. Sample programs

## 1. Roll the Dice (ET-57 Version)

The program uses the internal random number generator.

## Use :

| SBR | 1 | ... generates a random integer between 1 and 6 |
| :--- | :--- | :--- |

R/S ... next number

## Program :

| 00 | 861 | LbI 1 | subroutine start label |
| :---: | :---: | :---: | :--- |
| 01 | 43 | $($ | calculates (6 x Rand +1$)$, random number 1..6.9999 |
| 02 | 6 | 6 |  |
| 03 | 55 | x |  |
| 04 | 79 | Rand | random number from 0 to $0.99999 \ldots$ |
| 05 | 75 | + |  |
| 06 | 1 | 1 |  |
| 07 | 44 | $)$ |  |
| 08 | 49 | Int | integer part of the number |
| 09 | -61 | INV SBR | end of subroutine |
| 10 | 511 | GTO 1 | next number with R/S |

## 2. Roll the Dice (TI-57 Version)

Since the original TI-57 did not have a Rand (random number generator) function, the latter's dice-rolling program cost twice the number of steps, plus the use of a register. (this program is also applicable, with some minor variations, to the successor models of the TI-57, namely the TI-57 LCD, TI-57 II and TI-62).

## Register :

R0 ... Random number generator seed.

## Use:

$\times$ STO 1 ... initialize the number generator with a seed $=x$

| SBR 1 ... generates a random integer between 1 and 6 |
| :--- | :--- |

R/S .. next number

## Program :

| 00 | 861 | Lbl 1 | subroutine start label |
| :---: | :---: | :---: | :---: |
| 01 | 43 | ( |  |
| 02 | 43 | $($ | $\backslash$ |
| 03 | 330 | RCL 0 | \| Recall seed |
| 04 | 75 | + | \| |
| 05 | 30 | pi | \| |
| 06 | 44 | ) | 1 |
| 07 | 35 | $y^{\wedge} x$ | > Calculation of frac ( Seed +pi$)^{\wedge} 8$ ) |
| 08 | 8 | 8 | \| |
| 09 | 44 | ) | \| |
| 10 | 43 | $($ | \| |
| 11 | -49 | INV Int | / |
| 12 | 320 | STO 0 | Stores the new seed (Seed) |
| 13 | 55 | x | \} |
| 14 | 6 | 6 | \| |
| 15 | 75 | + | > Dice value from 1 to 6 |
| 16 | 1 | 1 | \| |
| 17 | 44 | ) | / |
| 18 | 49 | Int |  |
| 19 | -61 | INV SBR |  |
| 20 | 511 | GTO 1 | next number with R/S |

## 3. LED light snake

The program controls an external device - the ERAM100 effect frame. By writing a byte to port 0,8 LEDs are controlled. The byte written is a combination of bits lighting up individual LEDs, like the sum of the weights of the bits :

- bit 0 ... weight 1
... LED 1
- bit 4 ... weight 16 ... LED 5
- bit 1 ... weight 2
... LED 2
- bit 5 ... weight 32 ... LED 6
- bit 2 ... weight 4
... LED 3
- bit 6 ... weight 64 ... LED 7
- bit 3 ... weight 8
... LED 4
- bit 7 ... weight 128 ... LED 8


## Use:

RST R/S ... start the snake :
3 bright LEDs run along the LED strip

## Registers:

R5
... save snake position
R8 ... index, -1 is the index of port 0 (output to LED)

## Program :

| 00 | 7 | 7 | bits value of snake appearance (LED 1,2,3 lights up) |
| :---: | :---: | :---: | :---: |
| 01 | 325 | STO 5 | Stores snake's position |
| 02 | 1 | 1 |  |
| 03 | 84 | +/- |  |
| 04 | 328 | STO 8 | sets the index of R8 to -1, which is the address of port 0 |
| 05 | 2 | 2 |  |
| 06 | 5 | 5 |  |
| 07 | 6 | 6 |  |
| 08 | 22 | $x<>t$ | store 256 in T for pattern overflow test |
| 09 | 869 | Lbl 9 | cycle start label |
| 10 | 335 | RCL 5 | recall of the position of the snake |
| 11 | 55 | x |  |
| 12 | 2 | 2 |  |
| 13 | 85 | $=$ | (position $\times 2$ ) corresponds to a shift of 1 bit to the left |
| 14 | -76 | INV $\mathrm{x}>=\mathrm{t}$ | location < 256? |
| 15 | 518 | GTO 8 | no position overflow, go to Lbl 8 |
| 16 | 65 | - |  |
| 17 | 2 | 2 |  |
| 18 | 5 | 5 |  |
| 19 | 5 | 5 |  |
| 20 | 85 | $=$ | rotation: - 256 (remove bit 7$)+1($ add bit 0$)$ |
| 21 | 868 | Lbl 8 |  |
| 22 | 325 | STO 5 | stores the snake's new position |
| 23 | 57 | STO* | storage at address -1 sends the byte to port 0 |
| 24 | 36 | Pause | small pause of 0.25 seconds |
| 25 | 519 | GTO 9 | loop repeat |

## 4. Calculation of the polynomial

The program calculates the value of the polynomial

$$
P(x)=a 0+a 1^{*} x+a 2^{*} x^{\wedge} 2+\ldots a n^{*} x^{\wedge} n
$$

of order n for the given x , if the coefficients a 0 to an are entered.

## Registers:

R0 ... Dsz iteration counter
R6 ... number of coefficients N (= polynomial order $\mathrm{n}+1$ )
R8 ... index register
R9 ... input x
R10 and following ... polynomial coefficients a0, a1, ... an (N coefficients)

## Use:

Example, polynomial $\mathrm{P}(\mathrm{x})=2-3 \mathrm{x}+\mathrm{x}^{\wedge} 2$ :
RST R/S ... start entering the coefficients
2 R/S ... enter the coefficient a0 $=2$
$3 \quad+/-\quad$ R/S $\quad .$. input of coefficient al $=-3$
1 R/S... coefficient input a2 $=1$

| 2 | SBR | $\mathbf{1}$ |
| :--- | :--- | :--- |


| 1 | $+/-$ | R/S | ... calculation of the value of the polynomial $P(-1)=6$ |
| :---: | :---: | :---: | :---: |

1 5 R/S ... calculation of the value of the polynomial $P(15)=182$

## Program :

| 00 | 15 | CLR | reset |
| :---: | :---: | :---: | :--- |
| 01 | 326 | STO 6 | reset of the number of coefficients N |
| 02 | 9 | 9 | index of the first coefficient 10-1 = 9 |
| 03 | 328 | STO 8 | index registry settings |
| 04 | 869 | Lbl 9 | loop labels for entering coefficients |
| 05 | 81 | R/S | stop the program, wait for the next coefficient |
| 06 | 778 | Inc 8 | increment index register R8 |
| 07 | 57 | STO* | store the coefficient |
| 08 | 776 | Inc 6 | incrementing the number of coefficients N |
| 09 | 519 | GTO 9 | continue with the next coefficient |


| 10 | 868 | Lbl 8 | calculation repeat label |
| :---: | :---: | :---: | :--- |
| 11 | 81 | R/S | display the result and wait for another ' $x$ ' |
| 12 | 861 | Lbl 1 | start label of the polynomial quantization function |
| 13 | 329 | STO 9 | save ' $x$ ' entered |
| 14 | 43 | ( |  |
| 15 | 336 | RCL 6 | number of coefficients N |
| 16 | 320 | STO 0 | Dsz counter preparation |
| 17 | 75 | + |  |
| 18 | 9 | 9 | N + 9 = index of the last coefficient an |
| 19 | 44 | ) |  |
| 20 | 328 | STO 8 | R8 index register setting |
| 21 | 58 | RCL* | recall the last coefficient an |
| 22 | 867 | Lbl 7 | loop start label |
| 23 | -56 | INV Dsz | decrement R0 and skip instruction when > 0 |
| 24 | 518 | GTO 8 | loop if R0 differs from 0 otherwise end of loop |
| 25 | -778 | INV Inc 8 | decrement index register R8 |
| $\#$ | 43 | ( |  |
| 27 | 14 | CE | Restore last X register |
| 28 | 55 | X |  |
| 29 | 339 | RCL 9 | Calculation Display * ' $x$ ' entered |
| 30 | 75 | + |  |
| 31 | 58 | RCL* | addition of another coefficient ai (from index R8) |
| 32 | 44 | ) |  |
| 33 | 517 | GTO 7 | continue the loop |

## 5. Complex numbers

Arithmetic of complex numbers.
When entering a number, enter the real part, press $\mathbf{x}<>\mathbf{t}$, and enter the imaginary part. In the $\mathbf{T}$ register (register $\mathbf{R 7}$ ) there will be the real part of the number, and in the $\mathbf{X}$ register (display) the imaginary part.
When reading the result, after pressing $\mathbf{x}<>\mathbf{t}$ you will read the real part, after pressing a second time on $\mathbf{x}<>\mathbf{t}$ you will read the imaginary part.

For 2-operand functions, specify the first operand (X) using SBR 1.
Then specify the second operand $(\mathbf{Y})$ and call the function.
The result simultaneously becomes the new first operand ( $\mathbf{X}$ ).
For 1-operand functions, specify the operand $(\mathbf{Y})$ and call the function.
The original first operand $(\mathbf{X})$ remains unchanged.
The program occupies 2 program spaces, Pgm 0 and Pgm 1.
Note : The $\ln (\mathrm{Y})$ and $\exp (\mathrm{Y})$ functions change the angular measure to radians.

## Use:

Program space Pgm 0 :

| SBR | 1 | ... input of the first operand |
| :---: | :---: | :---: |
| SBR | 2 | ... adding the second operand $X+Y$ |
| SBR | 3 | ... subtraction of the second operand X-Y |
| SBR | 4 | ... multiplication by the second operand $X * Y$ |
| SBR | 5 | ... division by the second operand X/Y |
| SBR | 6 | ... negation -Y |

Note: The SBR 5 function calls the SBR 1 function from Pgm 1.

## Program space Pgm 1 :

| SBR | 1 | ... inverse of $1 / Y$ |
| :---: | :---: | :---: |
| SBR | 2 | ... square of $\mathrm{Y}^{\wedge} 2$ |
| SBR | 3 | ... square root of sqrt(Y) |
| SBR | 4 | ... natural logarithm of $\ln (\mathrm{Y})$ |
| SBR | 5 | ... natural exponent exp(Y) |

Example: calculates $\exp (((2+3 \mathrm{i})-(1-\mathrm{i})) /(4+5 \mathrm{i}))$

Pgm 0


| 1 | $\mathrm{x}: \mathrm{t}$ | 1 | $+/-$ | SBR |
| :--- | :--- | :--- | :--- | :--- |

## x:t

x: t

x: t
x: 1
[0.2682...]
$\ldots$ intermediate result $=(0.5853 \ldots+0.2682 \ldots \mathrm{i})$
Pgm
1
[4]
$\ldots$ intermediate result $=(1+4 i)$
... division by operand ( $4+5 \mathrm{i}$ )
... selection of program space 1
... natural exponent exp (Y)
[1.7314...]
[0.4760...]
... result (1.7314... $+0.4760 . . i)$

## Registers:

R1 ... 'a', the real part of the first operand of $X$
R2 ... 'b', the imaginary part of the first operand of $X$
R3 ... 'c', the real part of the second operand of Y
R4 ... 'd', the imaginary part of the second operand $Y$
R7 ... T register

## Program :

Pgm 0 ... selection of program space 0

- calculation of the subtraction of the second operand X-Y

| 00 | 863 | Lbl 3 |
| :--- | :--- | :---: |
| 01 | 616 | SBR 6 | call the negation function $-Y$

- calculation of the second operand $X+Y$

$$
X+Y=(a+c)+(b+d) * i
$$

| 02 | 862 | LbI 2 | X+Y function label |
| :---: | :---: | :---: | :--- |
| 03 | 342 | SUM 2 | add the imaginary part of Y to $X$ |
| 04 | 332 | RCL 2 | recall of the imaginary part of $X$ |
| 05 | 22 | X<>t | exchange of real $<>$ imaginary parts |
| 06 | 341 | SUM 1 | add the real part of Y to $X$ |
| 07 | 331 | RCL 1 | recall of the real part of $X$ |
| 08 | 22 | x $<>t$ | exchange of real $<>$ imaginary parts |

- entering the first operand $X$

| 09 | 861 | Lbl 1 | X function label |
| :---: | :---: | :---: | :---: |
| 10 | 322 | STO 2 | store the imaginary part of $X$ |
| 11 | 22 | x<>t | exchange of real <> imaginary parts |
| 12 | 321 | STO 1 | store the real part of $X$ |
| 13 | 22 | x<>t | exchange of real <> imaginary parts |
| 14 | -61 | INV SBR |  |

- calculation of the division by the second operand $X / Y$

| 15 | 865 | Lbl 5 | X/Y function label |
| :--- | :--- | :--- | :--- |
| 16 | 781 | Pgm 1 | choice of program space 1 |
| 17 | 611 | SBR 1 | inverse function call of $1 / Y$ |

- calculation of the multiplication by the second operand $X * Y$

$$
X * Y=(a * c-b * d)+(a * d+b * c) * i
$$

| 18 | 864 | Lbl 4 | $X * Y$ function label |
| :---: | :---: | :---: | :---: |
| 19 | 324 | STO 4 | storage of the imaginary part $\mathrm{Y}(=\mathrm{d})$ |
| 20 | 22 | x<>t | exchange of real <> imaginary parts |
| 21 | 43 | ( |  |
| 22 | 323 | STO 3 | storage of the real part of $\mathrm{Y}(=\mathrm{c})$ |
| 23 | 55 | X |  |
| 24 | 331 | RCL 1 | real part of $X(=a)$ |
| 25 | 65 | - |  |
| 26 | 332 | RCL 2 | recall imaginary part of $\mathrm{X}(=\mathrm{b})$ |
| 27 | 55 | x |  |
| 28 | 334 | RCL 4 | recall imaginary part of $Y(=d)$ |
| 29 | 44 | ) | calculation (a*c-b*d) real part |
| 30 | 22 | $x<>t$ | exchange of real <> imaginary parts |
| 31 | 43 | ( |  |
| 32 | 331 | RCL 1 | recall of the real part of $\mathrm{X}(=a)$ |
| 33 | 55 | x |  |
| 34 | 334 | RCL 4 | recall imaginary part of $Y(=d)$ |
| 35 | 75 | + |  |
| 36 | 332 | RCL 2 | recall of the imaginary part $\mathrm{X}(=\mathrm{b})$ |
| 37 | 55 | X |  |
| 38 | 333 | RCL 3 | recall of the real part of $Y(=c)$ |
| 39 | 44 | ) | calculation ( $\mathrm{a}^{*}$ d $+\mathrm{b} * \mathrm{c}$ ) imaginary part |
| 40 | 511 | GTO 1 | store result in X |

- Change operator sign -Y

| 41 | 866 | Lbl 6 | -Y function label |
| :---: | :---: | :---: | :---: |
| 42 | 84 | $+/-$ | negation of the imaginary part |
| 43 | 22 | $x<>t$ | exchange of real $<>$ imaginary parts |
| 44 | 84 | $+/-$ | negation of the real part |
| 45 | 22 | $x<>t$ | exchange of real $<>$ imaginary parts |
| 46 | -61 | INV SBR |  |
|  |  |  |  |

- inverse of operand $1 / Y$

$$
1 / Y=\left(c-d^{*} i\right) /\left(c^{\wedge} 2+d^{\wedge} 2\right)
$$

| 00 | 861 | Lbl 1 | 1/Y function label |
| :---: | :---: | :---: | :---: |
| 01 | 43 | $($ |  |
| 02 | 84 | +/- | change sign imaginary part of $\mathrm{Y}(=\mathrm{d})$ |
| 03 | 45 | : |  |
| 04 | 43 | ( |  |
| 05 | 23 | $x^{\wedge} 2$ | $\mathrm{j}^{\wedge} 2$ |
| 06 | 75 | + |  |
| 07 | 22 | $x<>t$ |  |
| 08 | 323 | STO 3 | storage of the real part of $\mathrm{Y}(=\mathrm{c})$ |
| 09 | 23 | $x^{\wedge} 2$ | $\mathrm{c}^{\wedge} 2$ |
| 10 | 44 | ) | calculation ( $\left.c^{\wedge} 2+d^{\wedge} 2\right)$ |
| 11 | -39 3 | INV Prd 3 | divide c by ( $\left.c^{\wedge} 2+d^{\wedge} 2\right)$ |
| 12 | 44 | ) | end of calculation of the imaginary part |
| 13 | 22 | $x<>t$ | exchange of real <> imaginary parts |
| 14 | 333 | RCL 3 | reminder of the new real part |
| 15 | 22 | $x<>t$ | exchange of real <> imaginary parts |
| 16 | -61 | INV SBR |  |

- squaring operand $Y^{\wedge} 2$

| 17 | 862 | Lbl 2 | $\mathrm{Y}^{\wedge} 2$ function label |
| :---: | :---: | :---: | :---: |
| 18 | 43 | ( |  |
| 19 | -27 | INV P->R | convert to polar coordinates |
| 20 | 55 | X | the angle will be multiplied by *2 |
| 21 | 22 | $x<>t$ | exchange of real <> imaginary parts |
| 22 | 23 | $x^{\wedge} 2$ | squared radius |
| 23 | 869 | Lbl 9 |  |
| 24 | 22 | x<>t | exchange of real <> imaginary parts |
| 25 | 2 | 2 |  |
| 26 | 44 | ) | angle * 2 (or angle / 2) is calculated here |
| 27 | 27 | P->R | convert to cartesian coordinates |
| 28 | -61 | INV SBR |  |

- square root operand sqrt(Y)

| 29 | 862 | LbI 3 | sqrt(Y) function label |
| :---: | :---: | :---: | :--- |
| 30 | 43 | $($ |  |
| 31 | -27 | INV P->R | conversion to polar coordinates |
| 32 | 45 | $:$ | the angle will be divisible by $/ 2$ |
| 33 | 22 | $\mathrm{x}<>$ t | exchange of real <> imaginary parts |
| 34 | 24 | Vx | square root of radius |
| 35 | 519 | GTO 9 | realization of the function |

- natural logarithm of the operand $\ln (Y)$

| 36 | 864 | Lbl 4 | In(Y) function label |
| :---: | :---: | :---: | :--- |
| 37 | 60 | Rad | switch to radians |
| 38 | -27 | INV P->R | lonverts to polar coordinates |
| 39 | 22 | x<>t | exchange of real <> imaginary parts |
| 40 | 13 | Inx | logarithm of the radius |
| 41 | 22 | $x<>$ t | exchange of real $<>$ imaginary parts |
| 42 | -61 | INV SBR |  |

- natural exponent of the operand $\exp (\mathrm{Y})$

| 43 | 865 | Lbl 5 | exp(Y) function label |
| :---: | :---: | :---: | :--- |
| 44 | 22 | x<>t | exchange of real <> imaginary parts |
| 45 | -13 | INV Inx | exponent exp(x) |
| 46 | 22 | x<>t | exchange of real <> imaginary parts |
| 47 | 60 | Rad | switch to radians |
| 48 | 27 | P->R | converts to Cartesian coordinates |
| 49 | -61 | INV SBR |  |

## 6. Ramanujan approximation of the factorial x!

Calculating the factorial (including decimals) using the Ramanujan approximation.
Accuracy achieved: Values around 1 precision 3 digits, values around 69 (maximum) precision 10 digits.

$$
\text { Formula : } x!=\operatorname{sqrt}(\mathrm{pi}) *(x / e)^{\wedge} x *\left(\left(\left(8^{*} x+4\right)^{*} x+1\right)^{*} x+1 / 30\right)^{\wedge}(1 / 6)
$$

## Use:

$\mathbf{x}$ SBR 1 ... calculates the factorial x !
$\mathbf{x}^{\prime}$ R/S ... calculates for another number

## Examples:

| 1 | SBR | 1 |  | $\ldots \mathrm{l}$ ! $=1,00028 \ldots$, the correct valmue must be 1,0 |
| :---: | :---: | :---: | :---: | :---: |
| 1 | - | 2 | R/S | $\ldots 1.2!=1,101987 \ldots$, must be $1,101802 \ldots$ |
| 1 | 0 | R/S |  | ... $10!=3628800.3116$, must be 3628800 |
| 6 | 9 | R/S |  | $\ldots \mathrm{l}$. $69!=1,7112245244+98$, must be 1,7112245243+98 |

## Register :

R1 ... entered value of $x$

| 00 | 861 | Lbl 1 | start of program |
| :---: | :---: | :---: | :---: |
| 01 | 43 | ( |  |
| 02 | 43 | $($ |  |
| 03 | 321 | STO 1 | store input value |
| 04 | 45 | : |  |
| 05 | 1 | 1 |  |
| 06 | -13 | INV Inx | calculation of the constant e |
| 07 | 44 | ) | calculation of $\mathrm{x} / \mathrm{e}$ |
| 08 | 35 | $y^{\wedge} \mathrm{x}$ |  |
| 09 | 331 | RCL 1 | calculation of (x/e)^x |
| 10 | 55 | x |  |
| 11 | 30 | pi |  |
| 12 | 24 | Vx | pi square root calculation |
| 13 | 55 | x |  |
| 14 | 43 | $($ |  |
| 15 | 43 | ( |  |
| 16 | 43 | $($ |  |
| 17 | 8 | 8 |  |
| 18 | 55 | x |  |
| 19 | 331 | RCL 1 | calculation of 8 * x |
| 20 | 75 | + |  |
| 21 | 4 | 4 |  |
| 22 | 44 | ) | calculation of (8*x +4 ) |
| 23 | 55 | x |  |
| 24 | 331 | RCL 1 |  |
| 25 | 75 | + |  |
| 26 | 1 | 1 |  |
| 27 | 44 | ) | calculation of ((8*x +4$\left.)^{*} x+1\right)$ |
| 28 | 55 | x |  |
| 29 | 331 | RCL1 |  |
| 30 | 75 | + |  |
| 31 | 3 | 3 |  |
| 32 | 0 | 0 |  |
| 33 | 25 | 1/x |  |
| 34 | 44 | ) | calculation of ...*x $+1 / 30$ ) |
| 35 | -35 | INV $y^{\wedge} \mathrm{x}$ | 6th root |
| 36 | 6 | 6 |  |
| 37 | 44 | ) |  |
| 38 | -61 | INV SBR |  |
| 39 | 511 | GTO 1 | repeat the calculation for another value |

## 7. Stirling approximation of the factorial $\ln (x!)$

Calculating the factorial (including decimals) using Stirling's approximation.
Accuracy achieved: Values around 1 3-digit precision, values around 69 (maximum x!)
10-digit precision, values around 200 15-digit precision.
Formula $: \ln (x!)=x^{*} \ln (x)+\ln (\operatorname{sqrt}(2 * p i))-x+\ln \left(\operatorname{sqrt}\left(x+1 / 6+1 / 72 / x-31 / 6480 / x^{\wedge} 2\right)\right)$.

## Use:

$\mathbf{x}$| $\mathbf{S B R}$ | 1 | calculates the logarithm of the factorial $\ln (x!)$ |
| :---: | :---: | :---: | :---: | :---: | :---: |

$\mathbf{x}^{\prime}$ R/S ... calculates for another number

$\mathbf{x}^{\prime}$ R/S ... calculates for another number

## Examples:

1 SBR 2 ... $1!=0.99990 \ldots$, the correct value must be 1,0

| 1 | . | 2 | R/S |  | $1.2!=1.10177 \ldots$, must be 1,101802 |
| :---: | :---: | :---: | :---: | :---: | :---: |

$1 \quad 0 \quad$ R/S $\quad . .10!=3628800.1322$, must be 3628800
$6 \quad 9 \quad$ R/S $\quad . .69!=1.7112245243+98$, correct value

1 | 1 | 0 | $\mathbf{S B R}$ | $\mathbf{1}$ | $\ldots \ln (1000!)=5912.1281785$, correct value |
| :--- | :--- | :--- | :--- | :--- |

## Register :

R1 ... entered value of $x$

## Program :

- calculation of $\ln (x!)$

| 0 | 811 | Lbl 1 | start of program $\ln (x!)$ |
| :---: | :---: | :---: | :---: |
| 1 | 43 | ( |  |
| 2 | 321 | STO 1 | store the entered value of $x$ |
| 3 | 55 | x |  |
| 4 | 13 | $\ln x$ | calculation of $x^{*} \ln (x)$ |
| 5 | 75 | + |  |
| 6 | 43 | $($ |  |
| 7 | 2 | 2 |  |
| 8 | 55 | x |  |
| 9 | 30 | pi |  |
| 10 | 44 | ) |  |
| 11 | 24 | Vx |  |
| 12 | 13 | $\ln x$ | calculation of $\ln (\mathrm{sqrt}(2 * \mathrm{pi})$ ) |
| 13 | 65 | - |  |
| 14 | 331 | RCL 1 | Recall x |
| 15 | 75 | + |  |
| 16 | 43 | ( |  |
| 17 | 331 | RCL 1 | Recall x |
| 18 | 75 | + |  |
| 19 | 6 | 6 |  |
| 20 | 25 | 1/x | number + 1/6 |
| 21 | 75 | + |  |
| 22 | 7 | 7 |  |
| 23 | 2 | 2 |  |
| 24 | 25 | 1/x |  |
| 25 | 45 | . |  |
| 26 | 331 | RCL 1 | number $+1 / 72 / \mathrm{x}$ |
| 27 | 65 | - |  |
| 28 | 3 | 3 |  |
| 29 | 1 | 1 |  |
| 30 | 45 | : |  |
| 31 | 6 | 6 |  |
| 32 | 4 | 4 |  |
| 33 | 8 | 8 |  |
| 34 | 0 | 0 |  |
| 35 | 45 | : |  |
| 36 | 331 | RCL 1 |  |
| 37 | 23 | $\mathrm{x}^{\wedge} 2$ | number - $31 / 6480 / x^{\wedge} 2$ |
| 38 | 44 | ) |  |
| 39 | 24 | Vx | square root of total |
| 40 | 13 | $\ln x$ |  |
| 41 | 44 | ) |  |
| 42 | -61 | INV SBR |  |
| 43 | 511 | GTO 1 | repeat the calculation for another value |

- calculation of $x$ ! [i.e. $e^{\wedge} \ln (x!)$ ]

| 44 | 862 | LbI 2 |  |
| :---: | :---: | :---: | :---: |
| 45 | 611 | SBR 1 | call function $\ln (x!)$ |
| 46 | -13 | INV Inx | exponent, $x!=\mathrm{e}^{\wedge} \ln (x!)$ |
| 47 | -61 | INV SBR |  |
| 48 | 512 | GTO 2 | repeat the calculation for another value |

## 8. Determining the zeros of a function

The program searches for zero crossings of the user function. The program occupies program spaces Pgm $\mathbf{0}$ and $\mathbf{P g m}$ 1. The user function is entered into program space Pgm 2 and marked with label Lbl 0. The function can temporarily use register R7 (register $\mathbf{T}$ ) and registers R10 and above.

The function first searches for a step interval $d x=(x m a x-x m i n) / 10$ in which the sign of $y$ changes. It then refines the place of passage by dividing the interval by zero until the deviation eps $=d x / 100000$. The size of the $d x$ step can be fixed at address 22 . With a large value of the $d x$ step, certain zero crossings can be skipped, a small value of $d x$ slows down the search. The magnitude of the eps deviation can be set at address 27. The eps value affects the zero crossing search accuracy achievable at the cost of slowing down the search.

## Use :

| SBR | 0 | ... user function: calculation of the value y for the given x |
| :--- | :--- | :--- |


| SBR | 1 | input of the lower limit of $x m i n$ |
| :--- | :--- | :--- |


... entering the upper limit of xmax
... determine the first zero crossing

... determine the next zero crossing

## Examples:

zeros of the function $f(x)=4^{*} \sin (x)+1-x$
The program for this function $f(x)$ must be created in the Pgm 2 space (see following pages).

| Pgm | 0 |  |  | ... selection of program space 0 |
| :---: | :---: | :---: | :---: | :---: |
| 3 | +/- | SBR | 1 | ... input of lower limit $x$ min $=-3$ |
| 3 | SBR | 2 |  | ... input of upper limit $\mathrm{xmax}=3$ |
| SBR | 3 |  |  | ... find the first zero crossing $=-2.2100 . .$. |
| SBR | 4 |  |  | ... find the second zero crossing $=-0.3421 .$. |
| SBR | 4 |  |  | ... find the third zero crossing $=2.7020 \ldots$ |
| SBR | 4 |  |  | ... fourth not found $=9.999+99$ |

## Registers:

RO ... the $y$ value of the tested function
R1 ... lower limit xmin
R2 ... upper limit of xmax
R3 ... delta interval dx
R4 ... $x$ the beginning of the interval
R5 ... $x$ end of interval
R6 ... x current
R7 ... T register, temporarily available for SBR 0
R8 ... eps deviation (minimum dx)
R9 ... current lower limit of xmin2

## Program :



- Calculation of the user function value

| 00 | 860 | LbI 0 |
| :---: | :---: | :---: |
| 01 | 782 | Pgm 2 |
| 02 | 610 | SBR 0 |
| choice of program space 2 |  |  |
| 03 | -61 | INV SBR |
|  | user function call |  |
|  |  |  |

- Entering the lower limit of $x m i n$

| 04 | 861 | Lbl 1 | entry of the lower limit xmin |
| :---: | :---: | :---: | :---: |
| 05 | 321 | STO 1 | stores the lower limit of $x \mathrm{~min}$ |
| 06 | -61 | INV SBR |  |

- Entering the upper limit of $x m i n$

| 07 | 862 | LbI 2 |
| :---: | :---: | :---: |
| 08 | 322 | STO 2 |
| 09 | -61 | INV SBR |
| stores of the upper limit of $x$ max |  |  |
|  |  |  |

- Display error : next not found

| 10 | 869 | Lbl 9 |
| :---: | :---: | :---: |
| 11 | 15 | CLR |
| 12 | 25 | $1 / x$ |
| 13 | 868 | Lbl 8 |
| 14 | -61 | causer display |

- Subroutine to find the first zero

| 15 | 863 | LbI 3 | first search for zero of the function |
| :---: | :---: | :---: | :--- |
| 16 | 332 | RCL 2 | recall upper limit xmax |
| 17 | 65 | - |  |
| 18 | 331 | RCL 1 | recall lower limit xmin |
| 19 | 329 | STO 9 | stores lower limit xmin |
| 20 | 85 | $=$ | calculates difference (xmax - xmin) |
| 21 | 45 | $:$ |  |
| 22 | 1 | 1 | <- size of the dx step |
| 23 | 0 | 0 |  |
| 24 | 85 | $=$ | calculates dx = interval/10 |
| 25 | 323 | STO 3 | stores delta dx interval |
| 26 | 45 | $:$ |  |
| 27 | 5 | 5 | <- amplitude of the eps deviation |
| 28 | -18 | INV log | constant 100000 |
| 29 | 85 | $=$ | calculates eps maximum deviation |
| 30 | 328 | STO 8 | stores eps deviation |

- Subroutine to find next zero

| 31 | 863 | LbI 4 | another zero search function |
| :---: | :---: | :---: | :--- |
| 32 | 332 | RCL 2 | recall upper limit of xmax |
| 33 | 22 | x<>t | xmax in T |
| 34 | 339 | RCL 9 | recall lower limit xmin updated |
| 35 | 76 | x>=t | upper limit reached? |
| 36 | 519 | GTO 9 | next passage not found |
| 37 | 324 | STO 4 | store x interval start |
| 38 | 75 | + |  |
| 39 | 333 | RCL 3 | dx delta interval reminder |
| 40 | 85 | $=$ |  |
| 41 | 329 | STO 9 | stores new xmin lower limit |
| 42 | 325 | STO 5 | stores x at end of interval |
| 43 | 610 | SBR 0 | calculates y at the end of the interval |
| 44 | 320 | STO 0 | stores value of y at the end of the interval |
| 45 | 334 | RCL 4 | recall x at start of interval |
| 46 | 326 | STO 6 | stores new updated x |
| 47 | 610 | SBR 0 | calculates y for the new updated $x$ |
| 48 | 781 | Pgm 1 | choice of program space 1 |
| 49 | 519 | GTO 9 | continuation of the function in space 1 |

$\square$ ... selection of program space 1

- Continuation of the search operation for the next zero

| 00 | 869 | Lbl 9 | continuation of the search for the next zero |
| :---: | :---: | :---: | :--- |
| 01 | 19 | C.t | reset T <br> 02 |
| 03 | 66 | x=t | is the value of y equal to 0 ? |
| 04 | 55 | GTO 8 | zero value found |
| 05 | 380 | Exc 0 | y_current * y_initial |
| 06 | 85 | $=$ |  |
| 07 | -76 | INV x>=t | if multiple < 0, zero found |
| 08 | 517 | GTO 7 | if zero found, refine result |
| 09 | 780 | Pgm 0 | switch to program space 0 |
| 10 | 514 | GTO 4 | continue with next interval |

- Loop to refine the result

| 11 | 867 | Lbl 7 | refining precision of zero found |
| :---: | :---: | :---: | :---: |
| 12 | 334 | RCL 4 | $x$ at start of interval |
| 13 | 75 | + |  |
| 14 | 335 | RCL 5 | $x$ at the end of the interval |
| 15 | 85 | = |  |
| 16 | 45 | : |  |
| 17 | 2 | 2 |  |
| 18 | 85 | $=$ | calculates center of the interval x |
| 19 | 326 | STO 6 | stores new x updated |
| 20 | 338 | RCL 8 | recall ps deviation |
| 21 | 22 | $x<>t$ | stores eps deviation in T |
| 22 | 335 | RCL 5 | recall $x$ at the end of the interval |
| 23 | 65 | - |  |
| 24 | 334 | RCL 4 | recall $x$ at start of the interval |
| 25 | 85 | = | calculates interval length |
| 26 | -76 | INV $\mathrm{x}>=$ t | interval < epsilon? |
| 27 | 516 | GTO 6 | if interval < epsilon, zero found OK |
| 28 | 336 | RCL 6 | recall x updated (interval center) |
| 29 | 782 | Pgm 2 | choice of program space 2 |
| 30 | 610 | SBR 0 | calculates y for the new x |
| 31 | 55 | $\times$ |  |
| 32 | 337 | RCL 0 | recall previous y |
| 33 | 85 | = |  |
| 34 | 19 | C.t | reset T |
| 35 | 66 | $\mathrm{x}=\mathrm{t}$ | $y=0$ ? |
| 36 | 516 | GTO 6 | zero found |
| 37 | 76 | $x>=t$ | if product > 0 , no sign change |
| 38 | 515 | GTO 5 | no sign change, move to higher x |
| 39 | 336 | RCL 6 | recall x updated (interval center) |
| 40 | 325 | STO 5 | shift down, the middle will be the new end |
| 41 | 517 | GTO 7 | continuation of the zero refinement loop |
| 42 | 865 | Lbl 5 | label to move to a higher $x$ |
| 43 | 336 | RCL 6 | recall x updated (interval center) |
| 44 | 324 | STO 4 | go up, the center will be a new beginning |
| 45 | 517 | GTO 7 | continuation of the zero refinement loop |
| 46 | 866 | Lbl 6 | OK result |
| 47 | 336 | RCL 6 | recall result |
| 48 | 780 | Pgm 0 | choice of program space 0 |
| 49 | 518 | GTO 8 | function return |

- example of user function $f(x)=4 * \sin (x)+1-x$

| 00 | 860 | Lbl 0 | user function label : must be Lbl 0 |
| :---: | :---: | :---: | :---: |
| 01 | 43 | ( |  |
| 02 | 327 | STO 7 | stores initial X |
| 03 | 60 | Rad | switch to radians |
| 04 | 28 | sin | , |
| 05 | 55 | x | \| |
| 06 | 4 | 4 | \| |
| 07 | 75 | + | > user function 4* $\sin (x)+1-x$ |
| 08 | 1 | 1 | \| |
| 09 | 65 | - | I |
| 10 | 337 | RCL 7 | \| |
| 11 | 44 | ) | / |
| 12 | -61 | INV SBR |  |

## 9. Simpson's rule for integration

The program calculates the numerical integral of the user function by Simpson's approximation. The program is stored in the program space $\mathbf{P g m} \mathbf{0}$, the user function is created in the program space Pgm 1 under the label Lbl 0.
The specified number of steps $n$ must be an even number.

## Use :

|  | CLR | RST | ... initialize operations and initialize program pointer |
| :---: | :---: | :---: | :---: |
| xmin | R/S |  | ... entering the lower limit |
| xmax | R/S |  | ... entering the upper limit |
| n | R/S |  | ... input of the number of steps (an even number!) and calculation |

## Examples:

integral of the function $f(x)=1 /(\cos (x)+2)$ in the nterval 0 to pi/2 The program for this function $f(x)$ must be created in the Pgm 2 space (see following pages).

| Pgm | 0 |  |  |  | ... selection of program space 0 <br> ... initialization operations and pointer reset (not 00) |
| :---: | :---: | :---: | :---: | :---: | :---: |
| CLR | RST |  |  |  |  |
| 0 | R/S |  |  |  | ... entering the lower limit |
| $\pi$ | $\div$ | 2 | = | R/S | ... entering the upper limit |
| 2 | 0 | R/S |  |  | ... entry of the number of steps (even!) and calculation [0.6046..] |

Result for 2 steps =
0.604998903 (3 digit accuracy)

Result for 4 steps =
Result for 10 steps =
Result for 20 steps = Result for 100 steps =
Result for 200 steps = Result for 1000 steps = Result for 2000 steps = Reference result =
0.604619709 (4 digit accuracy)
0.604600227 ( 6 digit accuracy)
0.604599815 (7 digit accuracy)
0.604599788 (10 digit accuracy)
0.604599788 (11 digit accuracy)
0.604599788 (13 digit accuracy)
0.604599788 (13 digit accuracy)
0.604599788

## Registers :

R0 ... number of steps n, loop counter
R1 ... lower limit xmin
R2 ... step increment dx
R3 ... loss of the result of the integral $y$

## Program :

| Pgm | $\mathbf{0}$ | ... selection of program space 0 |
| :--- | :--- | :--- |


| 0 | 321 | STO 1 | stores the lower limit of xmin |
| :---: | :---: | :---: | :---: |
| 1 | 81 | R/S | waiting for upper bound xmax |
| 2 | 65 | - |  |
| 3 | 331 | RCL 1 | recall lower limit xmin |
| 4 | 85 | = | calculates interval (xmax - xmin) |
| 5 | 322 | STO 2 | stores the interval |
| 6 | 81 | R/S | waiting for the number of steps |
| 7 | 320 | STO 0 | stores number of steps n |
| 8 | -392 | INV Prd 2 | calculates step increment: interval / n, |
| 9 | 619 | SBR 9 | calculates current $x$ and $y$ |
| 10 | 323 | STO 3 | stores result of integral I |
| 11 | 868 | Lbl 8 | start of calculation loop |
| 12 | -770 | INV Inc 0 | decrement the RO index of the loop |
| 13 | 619 | SBR 9 | calculates current $x$ and $y$ |
| 14 | 55 | X |  |
| 15 | 4 | 4 |  |
| 16 | 85 | = | calculates y * 4 |
| 17 | 343 | SUM 3 |  |
| 18 | -56 | INV Dsz | decrement register R0, jump if $>0$ |
| 19 | 517 | GTO 7 | go to end of loop when RO $=0$ |
| 20 | 619 | SBR 9 | calculates current $x$ and y |
| 21 | 55 | x |  |
| 22 | 2 | 2 |  |
| 23 | 85 | = | calculates y * 2 |
| 24 | 343 | SUM 3 |  |
| 25 | 518 | GTO 8 | next step in the loop |
| 26 | 867 | Lbl 7 | end of the loop |
| 27 | 619 | SBR 9 | calculates current $x$ and $y$ |
| 28 | 343 | SUM 3 |  |
| 29 | 332 | RCL 2 | dx interval reminder |
| 30 | 45 | : |  |
| 31 | 3 | 3 | calculates increment dx / 3*y |
| 32 | 55 | X |  |
| 33 | 333 | RCL 3 | loss of result y |
| 34 | 85 | = |  |
| 35 | 81 | R/S | stop, result display |
| 36 | 867 | Lbl 9 | displays the calculation of current $x$ and $y$ |
| 37 | 331 | RCL 1 | lower limit xmin |
| 38 | 75 | + |  |
| 39 | 330 | RCL 0 | step counter |
| 40 | 55 | X |  |
| 41 | 332 | RCL 2 | step increment dx |
| 42 | 85 | = | current coordinate calculates $x$ |
| 43 | 781 | Pgm 1 | choice of program space 1 |
| 44 | 510 | GTO 0 | go to user function |


| Pgm | 1 |
| :--- | :--- |
|  | ... selection of program space 1 |

- example of user function $f(x)=1 /(\cos (x)+2)$

| 00 | 860 | Lbl 0 |
| :---: | :---: | :---: |
| 01 | 60 | Rad |
| 02 | 29 | cos |
| 03 | 75 | + |
| 04 | 2 | 2 |
| 05 | 85 | $=$ |
| 06 | 25 | $1 / x$ |
| 07 | -61 | INV SBR |

## 10. Linear regression line

The program calculates the coefficients of the approximate linear regression line using the method of least squares. The pair of values $(X, Y)$ is entered using the statistical function Stat. The regression line has the form $\boldsymbol{y}=\boldsymbol{m}^{*} \boldsymbol{x}+\boldsymbol{b}$.

The coefficient ' $m$ ', i.e. the slope of the line, is calculated according to the formula $m=\left(\operatorname{sum}\left(x^{*} y\right)-\operatorname{sum}(x)^{*} \operatorname{sum}(y) / N\right) /\left(\operatorname{sum}\left(x^{\wedge} 2\right)-\operatorname{somme}(x)^{\wedge} 2 / N\right)$.
The coefficient 'b', i.e. the displacement of the line in the $Y$ direction, is calculated according to the formula $\boldsymbol{b}=(\operatorname{somme}(\boldsymbol{y})-\boldsymbol{m} * \operatorname{somme}(x)) / \mathbf{N}$.


## Use:

Enter the pairs ( $\mathrm{X}, \mathrm{Y}$ ) using the key
Stat

## CLR

RST ... program pointer initialization (step 00)
R/S
... calculates the coefficient 'm'
R/S
... calculates the coefficient 'b'

The following functions can only be called after calculating ' $m$ ' and ' $b$ '.
x
SBR
1
... calculation of $y$ for a given value of $x$
y
SBR
2 ... calculation of $x$ for a given value of $y$

## Example:

| CLR | INV | c.t | ... clear all registers $X$, RO à R79 |
| :--- | :--- | :--- | :--- |


| 1 | 0 | 1 | 0 | 3 | $x=t$ | 6 | 0 | 9 | Stat |
| :--- | :--- | :--- | :--- | :--- | :--- | :--- | :--- | :--- | :--- |

entry point $1(101.3,609)$

| 1 | 0 | 3 | $\cdot$ | 7 | $x=t$ | 6 | 2 | 6 | Stat |
| :--- | :--- | :--- | :--- | :--- | :--- | :--- | :--- | :--- | :--- |

... entry point $2(103.7,626)$

| 9 | 8 |  | 6 | $x$ | $6 t$ | 5 | 8 | 6 |
| :--- | :--- | :--- | :--- | :--- | :--- | :--- | :--- | :--- |

.. entry point $3(98,6,586)$

... entry point 4 (99.9, 594)

.. entry point $5(97.2,579)$

... program pointer initialization
... calculates coefficient $\mathrm{m}=7.4734325186$
... calculates coefficient $\mathrm{b}=-148.5063762$
... for $X=97 Y=576,41657811$
... for $X=104 Y=628,73060574$
... for $Y=580$ est $X=97,479488091$
... for $Y=630$ est $X=104,16985425$

## Registers:

| R0 | $\ldots$ number of elements N |
| :--- | :--- |
| R1 | $\ldots$ sum of y |
| R2 | $\ldots$ sum of $\mathrm{y}^{\wedge} 2$ |
| R3 | $\ldots$ sum of $x$ |
| R4 | $\ldots$ sum of $x^{\wedge} 2$ |
| R5 | .. sum of $x^{*} y$ |
| R7 | ... T-register |
| R8 | $\ldots$ calculated coefficient ' $m$ ' |
| R9 | $\ldots$ calculated coefficient ' $b$ ' |

## Program :

- calculation of 'm'

| 00 | 335 | RCL 5 | recall sum of $x^{*} y$ |
| :---: | :---: | :---: | :--- |
| 01 | 65 | - |  |
| 02 | 333 | RCL 3 | recall sum of $x$ |
| 03 | 55 | $x$ |  |
| 04 | 331 | RCL 1 | recall sum of $y$ |
| 05 | 45 | $:$ |  |
| 06 | 330 | RCL 0 | recall number of items $N$ |
| 07 | 85 | $=$ | $\left(\right.$ sum $\left.\left(x^{*} y\right)-\operatorname{sum}(x)^{*} \operatorname{sum}(y) / N\right)$ |
| 08 | 45 | $:$ |  |
| 09 | 43 | $($ |  |
| 10 | 334 | RCL 4 | recall sum of $x^{\wedge} 2$ |
| 11 | 65 | - |  |
| 12 | 333 | RCL 3 | recall sum of $x$ |
| 13 | 23 | $x^{\wedge} 2$ |  |
| 14 | 45 | $:$ |  |
| 15 | 330 | RCL 0 | recall number of items $N$ |
| 16 | 85 | $=$ |  |
| 17 | 328 | STO 8 | memorization of the coefficient $m$ |
| 18 | 81 | R/S | program stop, display $m$ |

- calculation of 'b'

| 19 | 331 | RCL 1 | recall sum of $y$ |
| :---: | :---: | :---: | :--- |
| 20 | 65 | - |  |
| 21 | 338 | RCL 8 | recall coefficient $m$ |
| 22 | 55 | $x$ |  |
| 23 | 333 | RCL 3 | recall sum of $x$ |
| 24 | 85 | $=$ |  |
| 25 | 45 | $:$ |  |
| 26 | 330 | RCL 0 | recall number of items $N$ |
| 27 | 85 | $=$ |  |
| 28 | 329 | STO 9 | memorization of the coefficient b |
| 29 | 81 | R/S | program stop, display $b$ |

- Calculation of $y$ for a given value of $x$

| 30 | 861 | Lbl 1 |
| :---: | :---: | :---: |
| 31 | 43 | $($ |
| 32 | 14 | CE |
| 33 | 55 | x |
| 34 | 338 | RCL 8 |
| 35 | 75 | + |
| 36 | 339 | RCL 9 |
| 37 | 44 | $)$ |
| 38 | -61 | INV SBR | recall coefficient m

- Calculation of $x$ for a given value of $y$

| 39 | 862 | Lbl 2 |
| :---: | :---: | :---: |
| 40 | 43 | $($ |
| 41 | 43 | $($ |
| 42 | 14 | CE |
| 43 | 65 | - |
| 44 | 339 | RCL 9 |
| 45 | 44 | $)$ |
| 46 | 45 | $\vdots$ |
| 47 | 338 | RCL 8 |
| 48 | 44 | $)$ |
| 49 | -61 | INV SBR | recall coefficient b coefficient m

